



# Trapezoidal Control Integrating the Losses of an Electric Car Power Train

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**Abstract:** In this paper, we present a modeling approach of the power chain based on the trapezoidal control, including the losses of the power train of an electric car. This modeling approach is parameterized leading to a problem of optimization of the parameters influencing the losses which leads to an improvement in the autonomy. This model approach is implanted under the simulation environment Matlab-Simulink. Simulation results are encouraging and opening track search for work optimization and experimental validation of the developed model.

**Keywords:** Trapezoidal Control, Electric Cars, Losses, Autonomy, Modeling, Simulations

## 1. Introduction

In this paper, we present a trapezoidal control strategy of a synchronous permanent magnet motor with axial flux, incorporating the losses of the power train of an electric car. The model developed is highly parameterized and poses a problem of parameters influencing losses optimization to improve the autonomy of the car. This control strategy is compatible to systemic design process of all motor-converter detailed in [1-5].

In this context the paper is organized in three parts to knowledge:

- The first part concerns the modeling of the components of the power chain under the Matlab-Simulink environment.
- The second part describes the different models coupling principle.
- The third part illustrates and describes the main results of simulations.

## 2. Principle of the Control Strategy

The trapezoidal command allow to impose phase currents with the back electromotive forces (technique of back electromotive force compensation) leading to a reduction in consumption for a stationary required driving power by the vehicle. Indeed, four control loops for providing the shape and amplitude of the ideal supply voltages of the motor. A control loop providing the amplitude of the reference currents and

three control current loop delivering the phase voltages supplying motor [1, 2].

## 3. Model of the Motor-Converter

The engine is powered by a two-level voltage inverter with IGBT. Each phase of the motor is equivalent to a resistor in series with an inductance and a back electromotive force. The three phase's voltage of the model is described by the following equations [1-5]:

$$u_1 = R \times i_1 + (L - M) \times \frac{di_1}{dt} + e_1 \quad (1)$$

$$u_2 = R \times i_1 + (L - M) \times \frac{di_2}{dt} + e_2 \quad (2)$$

$$u_3 = R \times i_3 + (L - M) \times \frac{di_3}{dt} + e_3 \quad (3)$$

Where  $R$ ,  $L$ ,  $M$  are respectively the resistance, inductance and mutual inductance of the motor,  $i_i$  and  $u_i$  are respectively the current and the voltage of the  $i$  phase.

The electromagnetic torque is given by the following relationship [1-12]:

$$T_{em} = \frac{1}{\Omega} (e_1 \times i_1 + e_2 \times i_2 + e_3 \times i_3) \quad (4)$$

Where  $e_i$  is the back electromotive force of the  $i$  phase.

The model of the motor-converter is implanted under the Matlab-Simulink environment according to the following block diagram:

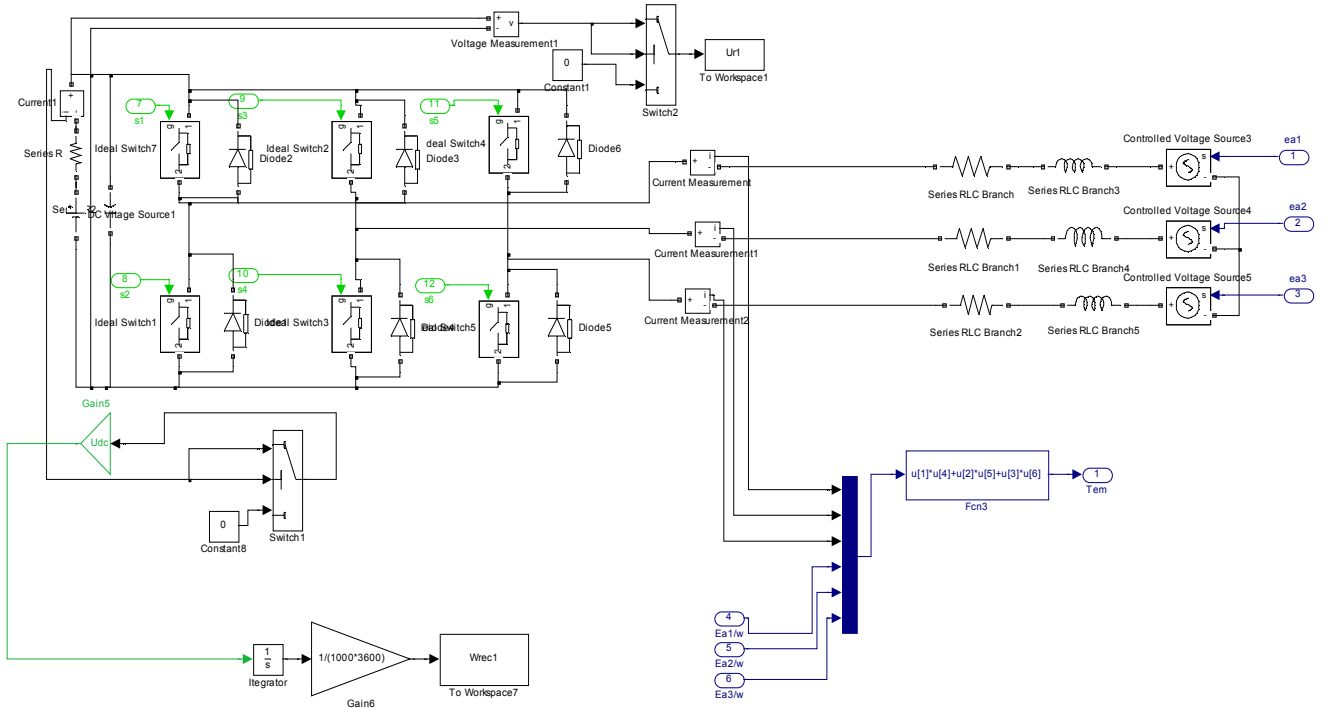


Figure 1. Simulink Model of the motor-converter.

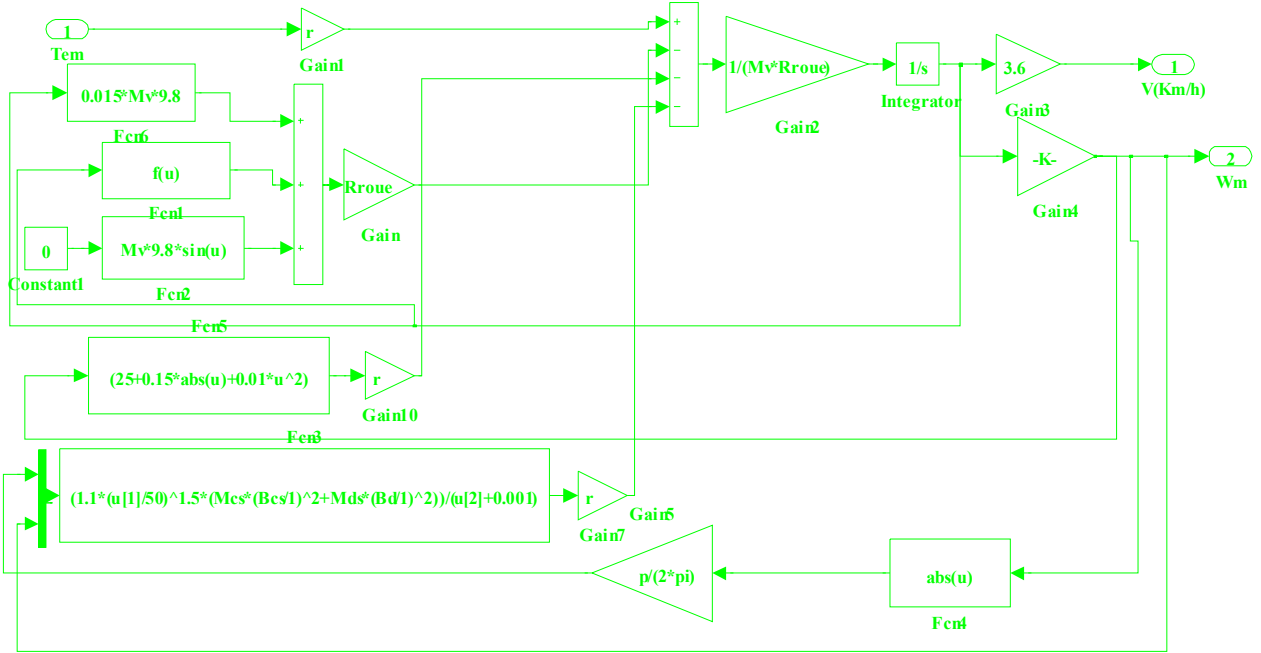


Figure 2. Simulink model of the motion equation.

#### 4. Equation of Movement

The vehicle motion equation is derived from the fundamental relationship of dynamics [1-12]:

$$(M_v \times R_r) \times \frac{dv}{dt} = r_d \times (T_{em} - T_f - T_{mec}) - (F_r + F_a + F_c) \times R_r \quad (5)$$

Where  $F_r$  is the rolling resistance force,  $F_a$  is the

aerodynamic force,  $F_c$  is the force of gravity,  $r_d$  is the amplification ratio,  $T_{em}$  is the electromagnetic torque,  $T_{fi}$  is iron losses torque,  $T_{mec}$  is the mechanical losses torque,  $R_r$  is the radius of the wheel of the car,  $v$  is the speed of the car and  $M_v$  and the mass of the car.

The equation of motion of the vehicle is implanted under the Matlab / Simulink environment according to the following figure:

## 5. Speed Regulator

The speed regulator allows to adjust the amplitude of reference currents. Indeed, the reference speed is compared to the response speed of the electric car. The output of the comparator drives a proportional integral regulator type for

providing the value of the reference currents amplitude minimizing the error between the reference speed and the response speed.

The Simulink model the speed regulator is illustrated by the following figure:

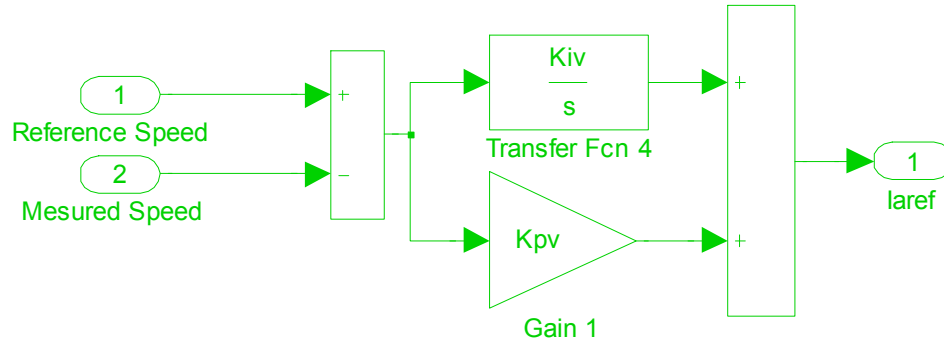


Figure 3. Speedregulator.

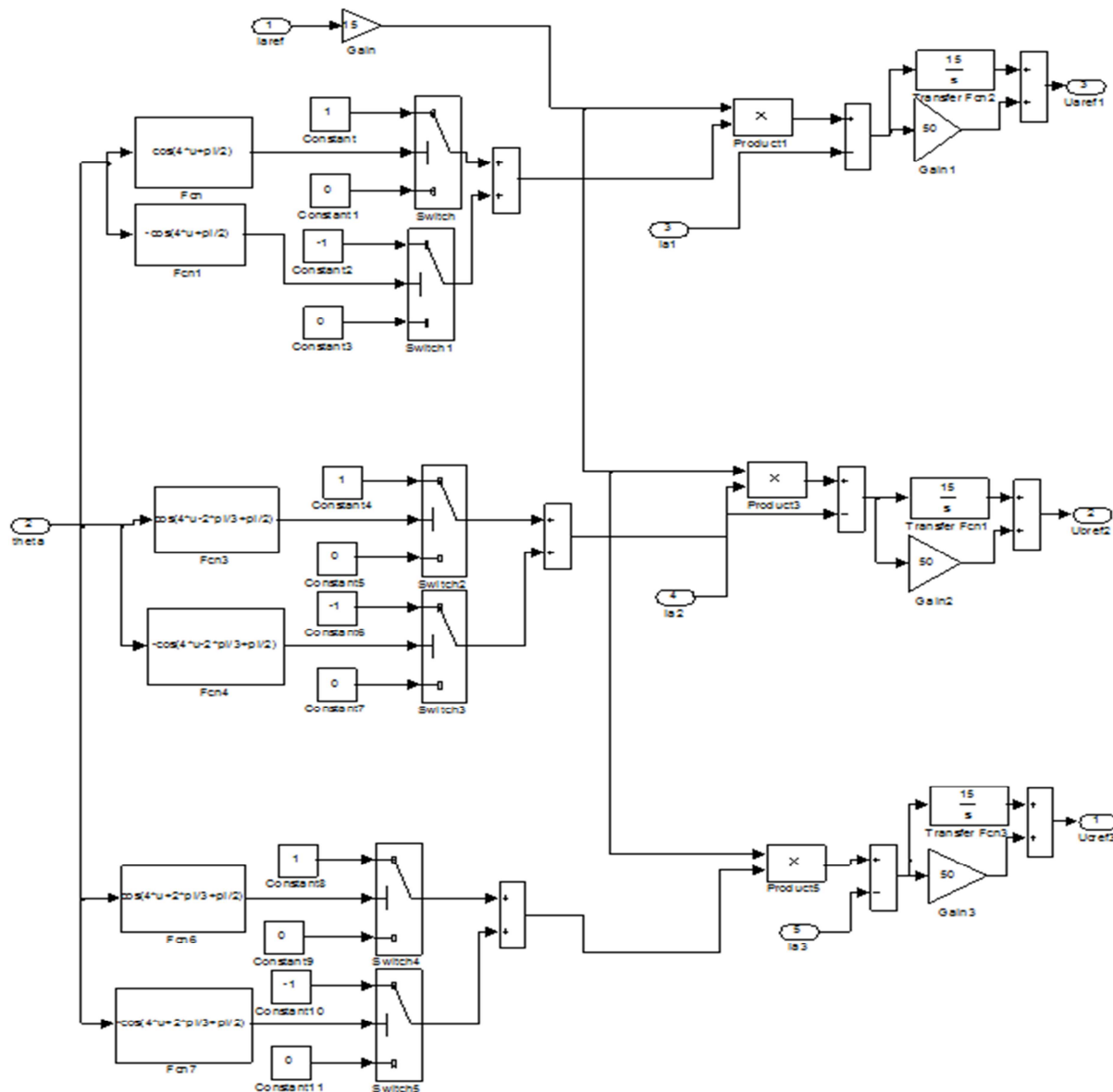


Figure 4. Simulink model of currents regulators.

## 6. Current Regulators

The reference current generator allows to generating three currents with trapezoidal shapes and phase shifted relative to each other by an angle equal to  $120^\circ$  electrical. This three phase currents are out in phase with back electromotive forces to minimize consumption and its amplitudes are controlled by the speed controller. Three control loops are used to convert currents to the three reference voltages of the motor. The model of the reference current generator is implanted under the Matlab / Simulink environment as shown in figure 4 [3].

## 7. Model of the Back Electromotive Forces

The three back electromotive forces are estimated from the following three equations:

$$a = \cos\left(p \times \Omega \times t + \frac{\pi}{2}\right) \quad (6)$$

$$b = \cos\left(p \times \Omega \times t - \frac{2 \times \pi}{3} + \frac{\pi}{2}\right) \quad (7)$$

$$c = \cos\left(p \times \Omega \times t - \frac{4 \times \pi}{3} + \frac{\pi}{2}\right) \quad (8)$$

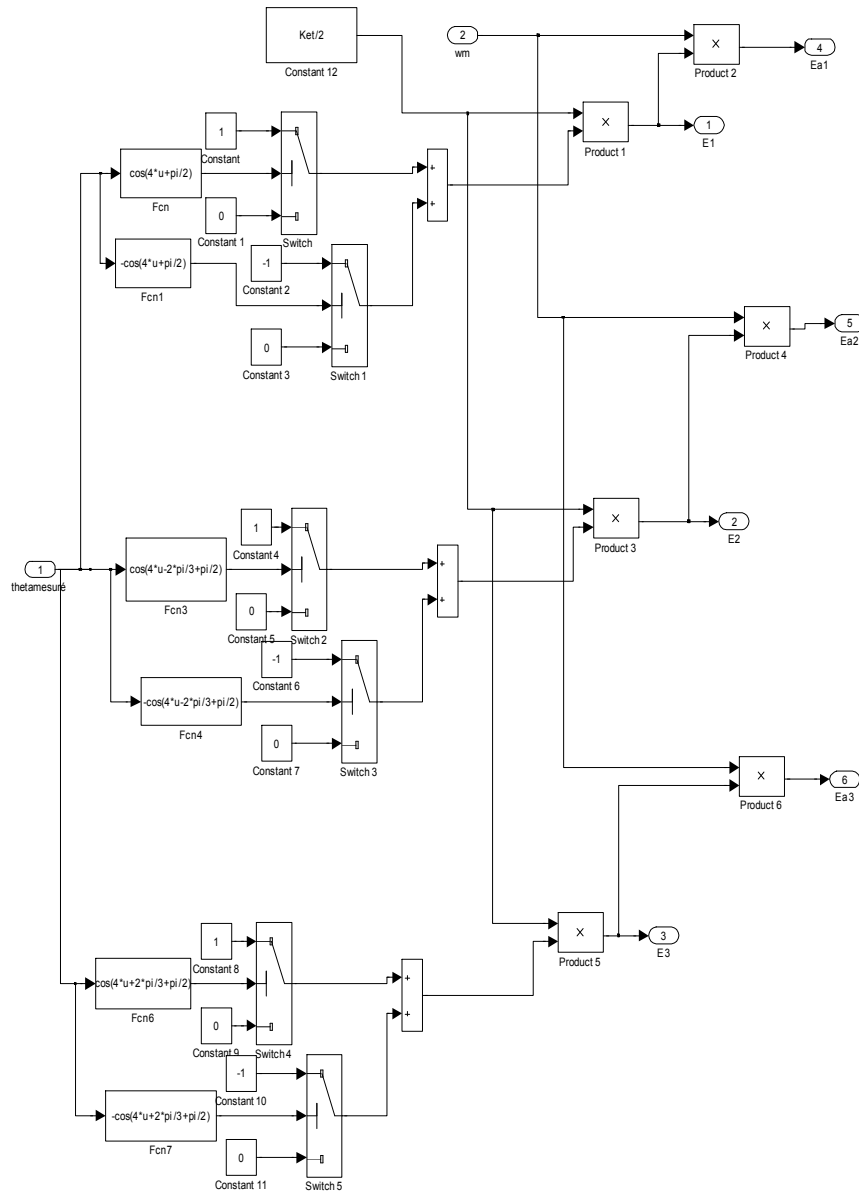


Figure 5. Simulink model of the back electromotive forces.

The models of the back electromotive forces ( $e_1$ ,  $e_2$ ,  $e_3$ ) are estimated from the following algorithm [3]:

```
{Begin
if
a>1/2;
a1=1/2.Ke.Ω;
else
a1=0;
if
a<-1/2;
a2=-1/2.Ke.Ω;
else
a2=0;
e1=a1+a2;
if
b>1/2;
b1=1/2.Ke.Ω;
else
b1=0;
if
b<-1/2;
```

```
b2=-1/2.Ke.Ω;
else
b2=0;
e2=b1+b2;
if
c>1/2;
c1=1/2.Ke.Ω;
else
c1=0;
if
c<-1/2;
c2=-1/2.Ke.Ω;
else
c2=0;
e3=c1+c2;
end}.
```

With  $K_e$  is the back electromotive constant and  $\Omega$  is the motor angular speed.

The Simulink model of the back electromotive forces is illustrated by the figure 5.

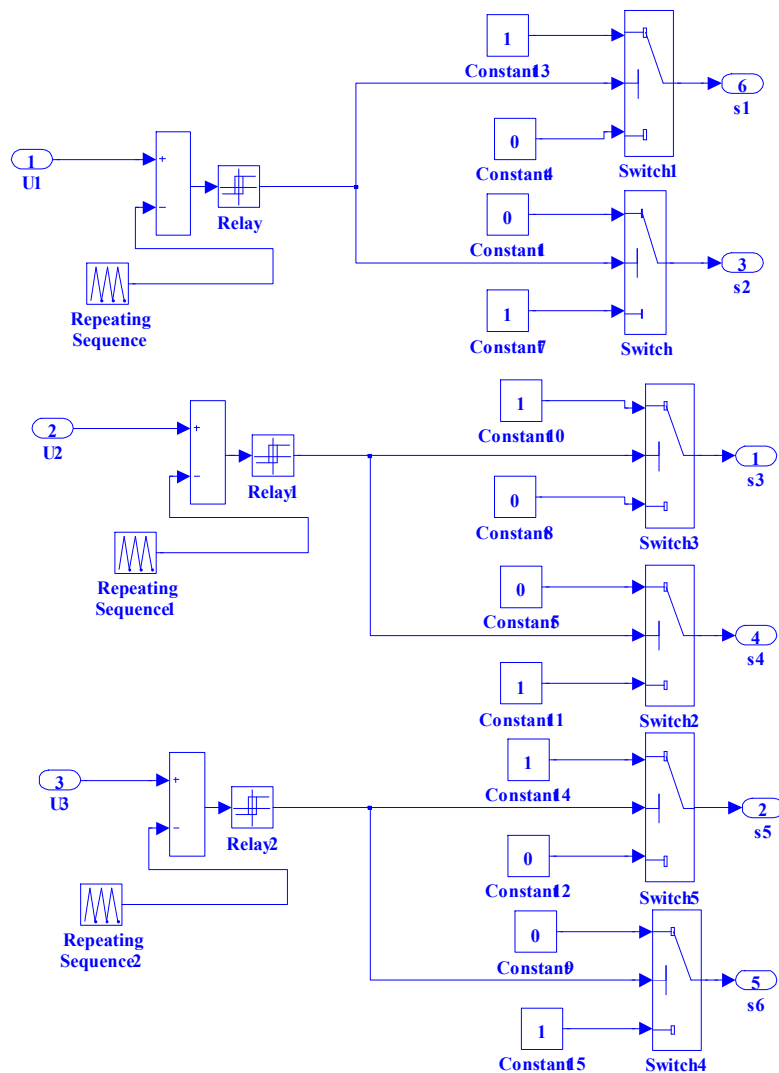
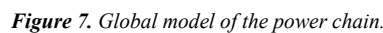


Figure 6. Simulink model of control signals generator.

The control signal generator compares the three reference voltages to a triangular signal with frequency significantly higher than the frequency of the voltages provided by the currents regulators. The output of each comparator attacks an hysteresis variant between 0 and 1 for outputting the signals for controlling the IGBTs S1, S3 and S5. The speed controller and current controller adjusts the pulse width of the control signals so as to impose currents in phase with the back electromotive forces and minimize the error between the reference speed and the speed of response. Signals for

## 9. Global Model of the Power Chain

The coupling of different models of the power train of the electric car leads to the overall model implanted under the Matlab / Simulink environment according to the figure 7.



The speed of response for a given travels is illustrated by the figure 8:

Figure 8 shows that the response speed follows with great accuracy the reference speed, which shows the effectiveness of the chosen control technology.

Figure 9 shows the evolution of the motor phase current.

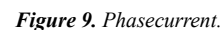
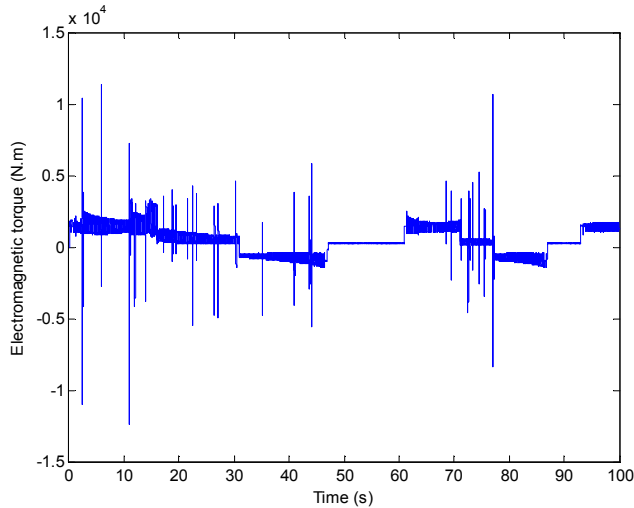


Figure 9 shows that the starting current is greatly reduced, leading to reduced energy consumption. This characteristic valid the performance of the selected control technology.

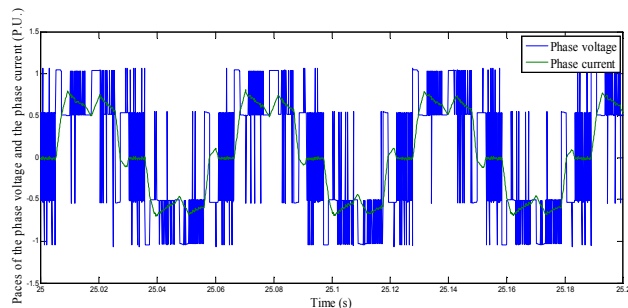
Figure 10 shows the evolution of the electromagnetic torque of the engine:



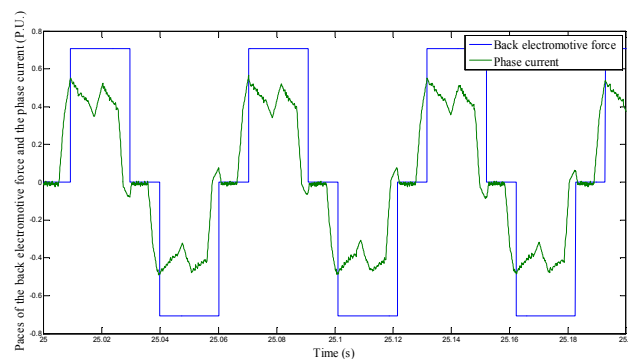
**Figure 10.** Electromagnetic torque.

The electromagnetic torque (Figure 10) has negative values since during generator operation phases, the engine torque is reversed.

Figure 11 shows the curves of the phase voltage and phase current.



**Figure 11.** Phases of the phase voltage and phase current.



**Figure 12.** Phases of the back electromotive force and the phase current.

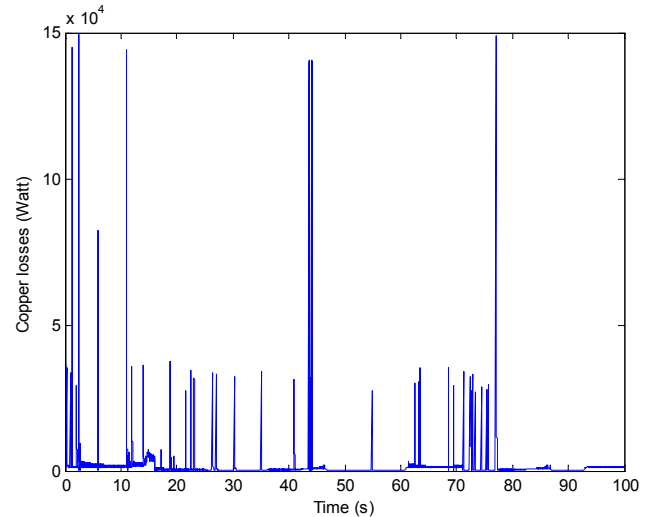
The shape of the phase current is close to a trapezoidal shape, which shows the effectiveness of the chosen control

technology.

Figure 12 illustrates the evolution of the back electromotive force and the phase current.

Figure 12 shows that there is a slight phase, reflecting the importance of the electric constant of the motor and low switching frequency.

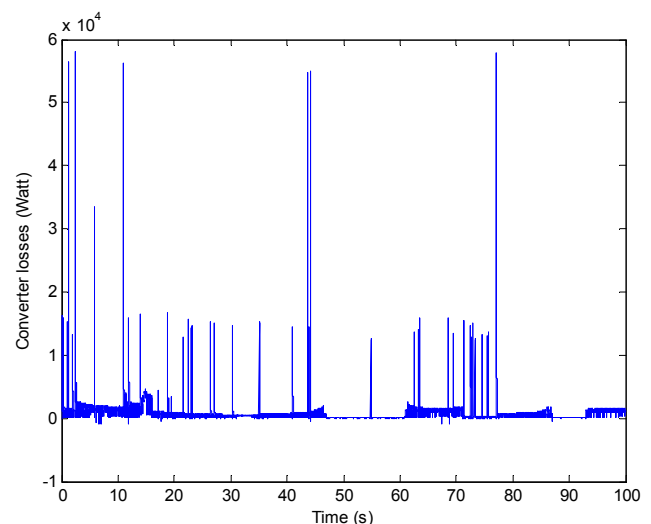
Figure 13 illustrates the evolution of copper losses [12].



**Figure 13.** Copper Losses.

The copper losses show peaks during heavy acceleration phases related to high stator currents. The average value of the copper losses is small view that the control technology imposes currents in phases with the back electromotive forces leading to a reduction current for a fixed power need.

Figure 14 illustrates the evolution of the losses in the inverter [12].

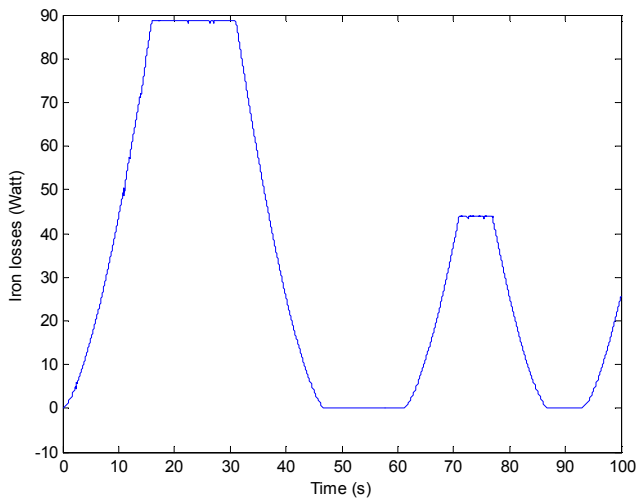


**Figure 14.** Inverter losses.

The losses in the inverter show peaks during heavy acceleration phases related to high stator currents. The average value of losses in the inverter is small view that the control technology imposes currents in phases with the back electromotive forces leading to a reduction of the phase

current for a fixed power need.

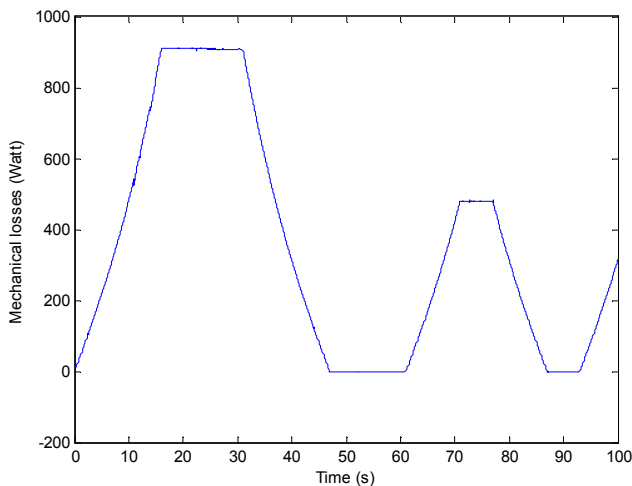
Figure 15 shows the evolution of the iron losses dissipated in the motor [12]:



**Figure 15.** Iron losses.

Figure 15 shows that the pace of the iron losses follows the curve of the speed since the iron losses are proportional to the frequency. These losses are small since the speed of the drive shaft is low (addition of a gear speed amplifier to reach the maximum speed).

Figure 16 illustrates the evolution of mechanical losses in the engine [12].



**Figure 16.** Mechanical losses.

The mechanical losses in the motor evolve in a shape close to the shape of the car's speed cycle since they are proportional to the speed.

## 11. Conclusion

A power chain modeling approach was presented based on the trapezoidal control, including the losses of the power train of an electric car. This modeling approach is parameterized, leading to a problem of optimization of the parameters

influencing the losses which leads to an improvement in the autonomy. This model approach is implanted under the simulation environment Matlab-Simulink. Simulation results are encouraging and open track search for work optimization and experimental validation of the developed model.

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