



# Comparing Two Classical Methods of Detecting Multicollinearity in Financial and Economic Time Series Data

Mutairu Oyewale Akintunde, Abolade Oludayo Olawale, Ajitoni Simeon Amusan, Adeyinka Ismail Abdul Azeez

Department of Statistics, School of Applied Sciences, Federal Polytechnic, Ede, Nigeria

## Email address:

waleakintunde2004@gmail.com (M. O. Akintunde)

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**Abstract:** Multicollinearity is an unavoidable problem being faced by researchers in financial and Economic data. It refers to a situation where the degrees of correlations between two or more independent variables are high. This is to say, one explanatory variable can be used in forecasting the other variable. This creates redundant information in a series under study, skewing the results in regression models. There is need to search for the source of the problem and proffering solution to this problem in Economics and Financial data. The data used was extracted from the record of Federal trade commission (FTC), 2019. The commission usually ranks annually arrays of locally made cigarettes in relation to Tar, nicotine and carbon monoxide components that was made available. Farrah-Glauber test and variance inflation factor were used as methods of detection multicollinearity in this paper. SPSS and J-multi packages were used to analyse the data collected for empirical illustration. The results of analysis indicated that variance inflation factor of  $X_1$  and  $X_2$  (Tar and Nicotine) are far above 10 (21.63 and 21.90) must be removed or collapsed from the model in order to correct multicollinearity. So, the preciseness of VIF made it to be preferred to Farrah-Glauber test. In line with the analysis, the use of Variance Inflation Factor is more preferred to Farrah-Glauber method. As VIF not only detected but also pointed to the direction of the problem.

**Keywords:** Multicollinearity, Farrah-Glauber, Predictor, Variance Inflation Factor, Financial and Economic Data, Regression Model

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## 1. Introduction

Multicollinearity refers to the circumstances where two or more independent variables in a statistical model are linearly related they are sometimes called collinearity: [1]. It is an important economic problem that has received several attentions globally but unfortunately the problem of resolving it has not yielded desire result. Of recent authors like [18, 15, 8, 2, 10, 11] researched into this econometric problem and established the danger the problem posed to the forecast ability of regression models. It is also regarded as economic problem that can lead to poor judgmental error and lead to poor economic policy formulation in financial time series the error is assumed to be independent and identically distributed whereas in the real-life situation most of the time is not so.

Multicollinearity among predictor variables has been attended to severally in econometric theory and in econometric texts (for examples., [6, 7, 19]. [9] Determines how collinearity upshots parameter coefficient instability in a measurement error situation. Many statistical models, notably those that are commonly use in ecology, finance, marine and Economics are liable to collinearity [3, 4, 17]. This occurs when too many variables have been pulled together in the model and a number of them measure similar phenomena. The existence of multicollinearity in a variable under study affects both the estimation of the parameters of the model and also gives rise to wrong interpretation of the results. Regression parameters estimates so obtained are compromised and may lead to instability, the estimated errors are extremely stretched and as a result inferences made based on these statistics are biased and lead to wrong policy formulation. However, for the models

that are not robust enough two problems are bound to happen under multicollinearity: any effects arising in the variable cannot be put apart variable effects cannot be separated and extrapolation or out of sample forecast is likely to be seriously erroneous and give a very wrong judgmental decision (s) [12].

Most introductory textbooks on statistics recognized multicollinearity as a problem principally associated with finance and Economics data. It is regarded as a situation where the model is not identified. As terrible as it is, several approaches for investigating it and working with it have been mapped out. Regardless of the peculiarities of the problem and the several available methods of solving them, most ecological, finance and Economics research have not made efforts to address this ubiquitous problem of multicollinearity [5, 16]: Non- addressing of these problem are directly linked to a very erroneous belief that statistical methods are not affected by multicollinear problems, ambiguity that surrounded the method to use couple with incompatible of a method in relation to the available data to be analysed, inability to interpret the results as a result of usage of approaches that incorporate variables or software that cannot be accessed. This problem is not only limited to ecology, finance and Economics [10, 13, 14].

The central objective of this paper is to provide a better perception of multicollinearity and to compare two methods (Farah-Glauber test and variance inflation method) of detecting its presence and determine the better one.

## 2. Mathematical Preliminaries

### 2.1. The Farrar and Glauber Test

This is a test to determine the presence as well as the degree of Multicollinearity in an equation. To achieve this objective a matrix of pair wise correlation coefficients is formed from the explanatory variables.

$$r_{ij} = \begin{bmatrix} 1 & r_{12} & r_{13} & \cdots & r_{1k} \\ r_{21} & 1 & r_{23} & \cdots & r_{2k} \\ \vdots & \vdots & \vdots & \cdots & \vdots \\ r_{ik} & r_{2k} & r_{3k} & \cdots & 1 \end{bmatrix}$$

This test is performed in three stages

- i. Chi-square test to determine or ascertain the existence and degree of multicollinearity.
- ii.  $F$ -test to locate the variable (s) that are intercorrelated, provided the test appeared positive.
- iii.  $t$ -test is use to determine the variable (s) that is (are) causing the multicollinearity problem provided the  $F$ -test is positive.

#### 2.1.1. Chi-Square Test

$H_0 : X$ 's are orthogonal, is a statistic predicated on the determinant  $|X'X|$  and could give a valuable measure of of the existence of multicollinearity in the explanatory variables. Bartlett (1937) obtained a transformation of  $|X'X|$

$$\chi^2 = -\left[N-1 - \frac{1}{6}(2K+5)\ln D\right]$$

This is distributed approximately as chi-square with  $v = \frac{1}{2}K(K-1)$  degrees of freedom; where  $K$  is the number of explanatory variables present in the series.  $S$

#### 2.1.2. $F$ -Test

If the Chi-square test confirmed the presence of Multicollinearity, we therefore, have no choice than to proceed to  $F$  - test using the following steps:

- i. List out the  $x_i$  considered to be inter-correlated with other  $x$ s as a function of  $x$ s . Therefore,

$$x_i = f(x_1, x_2, \dots, x_{i-1}, x_{i+1}, x_k) . \text{ Using data, we can write } x_i = \beta_2 X_2 + \beta_3 X_3 + U$$

- ii. Compute the parameter  $b_i = \begin{bmatrix} b_2 \\ b_3 \end{bmatrix}$

$$\text{As } b = (X'X)^{-1} X'X_1 \quad \text{where } X = (X_2 X_3)$$

$$\text{iii. Compute } R_i^2 = \frac{b_2 \sum X_1 X_2 + b_3 \sum X_1 X_3}{\sum X_1^2}$$

$$\text{Where } X_i X_j = \sum X_i X_j - \frac{\sum X_i \sum X_j}{N}$$

- iv. Compute the  $F$ -Statistic

$$F_{Calc.} = \frac{R_i^2 / (K-1)}{(1-R_i^2) / (T-K)} \quad \text{Check } F_\alpha(K-1, N-K) \quad F -$$

distribution table

#### 2.1.3. $t$ - Test

Having discovered that  $F$  test is positive. The  $t$  test is thereafter conducted to detect/examine which pair of variables are responsible for the multicollinearity. Suppose  $x_1$  is intercorrelated with  $x_2$  and  $x_3$  , under this condition, the  $t$  test is conducted as follows:

1. Define the hypothesis  
 $H_0 : x_2 \text{ and } x_3 \text{ are not responsible for multicollinearity against the}$   
 $H_1 : x_2 \text{ and } x_3 \text{ are responsible for multicollinearity .}$
2. Compute the partial coefficient of determination

$$r_{12.3}^2 = \frac{(r_{12} - r_{13}r_{23})^2}{(1-r_{13}^2)(1-r_{23}^2)} .$$

3. Define  $H_0 : r_{123} = 0$  against  $H_1 : r_{123} \neq 0$  .

4. Compute the statistic

$$t_{12} = \frac{r_{12.3} \sqrt{N-K}}{\sqrt{1-r_{12.3}^2}} \quad \text{and check } t_\alpha(N-K) \quad \text{from } t -$$

distribution table.

5. Repeat the test for  $x_1$  and  $x_3$  .

## 2.2. Variance Inflation Factor (VIF)

The aftermath of the multicollinearity is the rise in variance inflation factor. For the  $j$ th independent variable, the Variance Inflation Factor is given as

$$VIF_j = \frac{1}{1 - R_j^2}.$$

where  $R_j^2$  is the coefficient of determination when variable  $X_j$  is regressed on the  $j-1$  remaining explanatory variables, these factors are useful indicator in adjudging which of the variables may caused multicollinearity. Rule of thumb seems to be that we should be suspicious if any  $VIF_j > 5$  and positively horrified if  $VIF_j > 10$ . If this kind of result is obtained, a variable should be dropped or the model should be changed. if multicollinearity is discovered, theory and practical judgement should be used to pick the best variables to be kept in the model.

The sampling variance of the  $j$ th coefficient  $\hat{\beta}_j$  is

$$V(\hat{\beta}_j) = \frac{1}{(1 - R_j^2)(T-1)S_j^2}.$$

Where  $S_j^2 = \frac{\sum_{i=1}^T (X_{ij} - \bar{X}_j)^2}{(T-1)}$  is the variance of  $X_j$  and

$\sigma^2$  variance (Fox, 1997). The term  $\frac{1}{1 - R_j^2}$  indicates the

impact of multicollinearity on  $\hat{\beta}_j$ . It can be explained as the ratio of variance of  $\hat{\beta}_j$  to a supposed variance if  $X_j$  were uncorrelated with the remaining  $X_i$ .

## 3. Specification and Analysis of Data Used

The data used for this study was obtained from The Federal Trade commission (FTC), 2018, annually ranks varieties of domestic cigarettes according to their tar, nicotine and carbon monoxide contents.

### 3.1. Descriptive Statistics

Table 1. Descriptive Statistics.

STATISTIC	TAR	NICOTINE	WEIGHT
Mean	12.216	0.8764	0.9703
Standard Error	1.1332	0.0708	0.0175
Median	12.8	0.9	0.9573
Standard Deviation	5.6658	0.3541	0.0877
Sample Variance	32.1014	0.1254	0.0077
Kurtosis	2.9515	4.1604	0.4234
Skewness	0.7567	0.9690	0.4623
Sum	305.4	21.91	24.2571
Count	25	25	25

Table 1 describes reveal hidden statistics about the data used for the study, such statistics include, the mean, variance standard error kurtosis. Skewness and so on just to mention the few. The importance of all this information is to enrich would be policy makers, investors and academia on the associated properties of the data used. For example, Tar and

carbon could be both regarded as being approximately normal as their Kurtosis is less than 3, Nicotine is non-normal (Kurtosis greater than 3) as it possesses heavier tails compared to normal distribution. The skewness analysis show that the data are moderately skewed.

Table 2. Autocorrelation function (ACF).

Autocorrelations					
Series: y					
Lag	Autocorrelation	Std. Error <sup>a</sup>	Box-Ljung Statistic		
			Value	df	Sig. <sup>b</sup>
1	-.567	.192	8.724	1	.003
2	.145	.188	9.319	2	.009
3	-.180	.183	10.283	3	.016
4	.230	.179	11.929	4	.018
5	-.216	.174	13.455	5	.019
6	.099	.170	13.797	6	.032
7	-.005	.165	13.798	7	.055
8	-.042	.160	13.865	8	.085
9	.137	.155	14.648	9	.101
10	-.216	.150	16.724	10	.081
11	.222	.144	19.082	11	.060

Autocorrelations					
Series: y					
Lag	Autocorrelation	Std. Error <sup>a</sup>	Box-Ljung Statistic		
			Value	df	Sig. <sup>b</sup>
12	-.043	.139	19.177	12	.084
13	-.084	.133	19.580	13	.106
14	-.088	.127	20.064	14	.128
15	.156	.120	21.746	15	.115
16	-.018	.113	21.771	16	.151

a. The underlying process assumed is independence (white noise).  
b. Based on the asymptotic chi-square approximation.

Table 3. Partial Autocorrelation function (PACF).

Partial Autocorrelations		
Series: y		
Lag	Partial Autocorrelation	Std. Error
1	-.567	.204
2	-.260	.204
3	-.355	.204
4	-.077	.204
5	-.194	.204
6	-.205	.204
7	-.094	.204
8	-.218	.204
9	.060	.204
10	-.188	.204
11	.003	.204
12	.242	.204
13	-.008	.204
14	-.095	.204
15	-.096	.204
16	-.006	.204

Critical evaluation of the features exhibited by both ACF and PACF reveal that they contain 16 lags each, they slowly reduced exponentially. these features could be linked to the presence of multicollinearity or long memory in the series under study.

#### Fararr-Glauber Test

##### 3.1.1. Chi-square Test

$$r_{ij} = \begin{pmatrix} 1 & 0.98 & 0.49 \\ 0.98 & 1 & 0.50 \\ 0.49 & 0.50 & 1 \end{pmatrix}$$

$$\text{Det}(r_{ij}) = 0.05$$

$$\log_e 0.05 = -3.00$$

$$\chi^2_{\text{calculated}} = 66.51 \quad \chi^2_{0.05} 3 = 7.82$$

Since  $\chi^2_{\text{calculated}} > \chi^2_{0.05} 3$  i.e  $66.51 > 7.82$  . Therefore, multicollinearity exists.

##### 3.1.2. F – Test

Next is to carry out  $F$  – test to determine variable (s) causing multicollinearity

$$X_1 = f(X_2, X_3) \quad X_1 = \beta_2 X_2 + \beta_3 X_3 + U$$

$$\text{Thus, } \begin{bmatrix} \beta_2 \\ \beta_3 \end{bmatrix} = (X'X)^{-1} X'Y.$$

The values obtained from the analysis for  $\beta_2$  and  $\beta_3$  are

$$\begin{bmatrix} \beta_2 \\ \beta_3 \end{bmatrix} = \begin{bmatrix} 15.28 \\ 2.91 \end{bmatrix}$$

The  $F$  – computed is 206.52 and the tabulated value of  $F_{0.05} 2, 22 = 4.30$

Since  $F$  – computed is greater than  $F$  – tabulated we reject  $H_0$  and conclude that  $X_1$  is inter-correlated with  $X_2$  and  $X_3$  .

##### 3.1.3. t – Test

The following hypothesis were set up

$H_0$ :  $X_2$  and  $X_3$  are not responsible for multicollinearity

$H_1$ :  $X_2$  and  $X_3$  are responsible for multicollinearity

The value of  $T$  obtained from the analysis is 17.31, while the table value was 2.07.

Since computed value of  $T$  is greater than table value of  $T$  , we can conclude that  $X_2$  and  $X_3$  are responsible for multicollinearity.

##### 3.2. Variance Inflation Factor

The following values were obtained for VIF based on the

computer analysis.

**Table 4.** Parameters estimation and variance inflation factor.

Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.	Correlations			Collinearity Statistics	
	B	Std. Error	Beta			Zero-order	Partial	Part	Tolerance	VIF
(Constant)	3.202	3.462		.925	.365					
1 Tar	.963	.242	1.151	3.974	.001	.957	.655	.247	.046	21.631
Nicotine	-2.632	3.901	-.197	-.675	.507	.926	-.146	-.042	.046	21.900
Weight	-.130	3.885	-.002	-.034	.974	.464	-.007	-.002	.750	1.334

a. Dependent Variable: Carbon Monoxide

Table 4 above shows the value for  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  with its VIF value. From VIF value for Tar and Nicotine i.e  $X_1$  and  $X_2$  the value on the table is more than 10 which means multicollinearity exist.

Variable Selection Method

Existence of multicollinearity was established as shown in the above table 1, the next thing is how to correct it. To correct the existence of multicollinearity in the study, variable 3,  $X_2$  (Nicotine) was removed and the new VIF checked.

**Table 5.** New results obtained after excluding  $X_2$

Model	Unstandardized Coefficients		Standardized Coefficients	T	Sig.	Correlations			Collinearity Statistics	
	B	Std. Error	Beta			Zero-order	Partial	Part	Tolerance	VIF
(Constant)	3.114	3.416		.912	.372					
1 Tar	.804	.059	.961	13.622	.000	.957	.946	.838	.759	1.317
Weight	-.423	3.813	-.008	-.111	.913	.464	-.024	-.007	.759	1.317

a. Dependent Variable: Carbon Monoxide

Table 5 showing the values for  $\beta_0$ ,  $\beta_1$  and  $\beta_3$  with its VIF value. From VIF value for  $X_1$  and  $X_3$  the values obtained indicated that multicollinearity has vanished as none of VIF is up to 10.

**Table 6.** Compared the results obtained before and after dropping variable  $X_2$

	$\beta_0$	$\beta_1$	$\beta_2$	$\beta_3$	Remark
Multicollinearity with all variables	3.202	0.963	-2.632	-0.130	Presence of multi-collinearity ( $X_1$ and $X_2$ )
Standard error	(3.416)	(0.242)	(3.901)	(3.885)	
Variance Inflation factor		*21.631	*21.900	*1.334	
Multicollinearity When $X_2$ was excluded	3.114	0.804		-0.130	Multicollinearity disappeared.
Standard error	(3.416)	(0.059)		(3.813)	
Variance Inflation factor		*1.317		*1.317	

Table 6 above pooled together and compared the results obtained before and after variable  $X_2$  was excluded coupled with parameters estimate and standard errors. It is glaring that after the exclusion of the variable  $X_2$  the model becomes multi-collinearity free which fulfills the mission of the study.

## 4. Summary and Conclusion

So far, so good the study examines the descriptive nature of the series. Both the ACF and PACF decay exponentially establishing the fact that the series contain element of multicollinearity or long memory. Farrar-Glauber and variance information confirm the existence of multicollinearity. Having established this variable  $X_2$  was excluded and test re-conducted which after the analysis indicated that the multicollinearity earlier noticed had disappeared the preciseness of VIF made it to be preferred to Farrar-Glauber test. In line with the above assertion the use of Variance Inflation Factor is more preferred to Farrar-Glauber method. As VIF not only detected but also pointed to the direction of the problem.

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