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# Optimal Transmission Congestion Management with V2G in Smart Grid

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**Abstract:** The power system operators are looking for optimizing the power generating resources in the unit commitment problems considering the binding constraints. With the reconstruction in the power network structure, the increase in electricity price during some hours of day, and increase in fuel price, the utilities need to change their management paradigms. A smart grid can be a suitable choice for addressing these issues because they are able to continue working smartly. With the progress in the technology of batteries, power electronic devices, many well-known companies such as Toyota and Tesla have started producing electric and hybrid vehicles since 1990. Introducing electric vehicles to the power system provides unprecedented environmental and economic opportunities and at the same time new challenges to deal with for the system operators. The vehicle to grid (V2G) technology can enable the electric vehicles to inject energy to the grid in addition to its regular path of receiving energy from the grid. In this paper, the effect of the technology of V2G on the operation cost and LMP with considering the line congestion limits are investigated. To solve the optimization problem, a mixed integer linear programming (MILP) technique in the GAMS software is used. The proposed method is tested on the IEEE 6 bus system and the results are presented. This simulation shows that although the presence of electric vehicles has no significant effect on reducing or increasing of the operation cost in smart grid and may even reduce the operation cost in a certain number of EVs, due to their daily trips and shift from a bus to another bus, they act as a transmission line during the day and reduce the line congestion, resulting in a significant reduction in the local marginal price (LMP) in the peak load hours, and also increasing the security of the power system when the line capacity falls.

**Keywords:** EV, Line Congestion, V2G, Unit Commitment

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## 1. Introduction

Electric vehicles can be considered as loads and movable storage resources that are distributed in the entire power systems. The advent of modern power electronics has brought tremendous impact on power systems [1]. Power electronic interfaces facilitate the penetration of renewable energies into the smart grids [2]. Through voltage inverters Electric Vehicles work as potential source of energy in V2G mode. The V2G technology can also make the electric vehicles to contribute to the power generation during the peak hours and decrease the operation costs. Therefore, the increase in

penetration of the electric vehicles can have a significant influence on the operations of power systems. In [3], the economic benefits of electric vehicles in the ancillary services are investigated. In [4], the effects of charging PHEVs at charging stations are investigated and a strategy for improving the voltage profile and power factor in the distribution grid is proposed. In [5], aggregators are suggested to optimally control the electric vehicles when they are connected to the network. The plug-in hybrid electric vehicles (PHEVs) are considered as regulating power providers in two case studies in Germany and Sweden [6]. In [7, 8], the technology of energy storages and power electronic components for V2G

technology have been investigated. Electric vehicles consume energy based on the distance they travel, and it is possible that the total energy that electric vehicles receive are more than they deliver to the network [9]. In [10], the incorporation of electric vehicles in a V2G mode in the Western Danish power system is investigated. In [11], the electric vehicles are considered suitable for regulatory market, spinning storage, and ancillary services but not for the based load.

Most previous studies examined only economics and technical aspects of electric vehicles and not the effects of electric vehicles with V2G technology on the operation costs and local marginal price with considering the power flow limitations in power system lines. The goal of this paper is to model the electric vehicles with V2G technology in large scale as a distributed movable load, energy storage, and power generator and their effects on optimal operation with security constraints in power systems. In this paper, the word electric vehicle (EV) is, for simplicity, used instead of the electric vehicle with V2G technology.

The rest of this paper is organized as follows. In section 2, a brief description of smart grids and the effects of electric vehicles is presented. In section 2.2, the objective function is introduced. The V2G model used in the unit commitment is introduced in section 2.3. The results and discussion are presented in section 3. Finally, the conclusion and suggestions are presented in section 4.

## 2. Method

### 2.1. Smart Grid

Nowadays, most research institutes and utilities have realized that the smart grid is a necessity for power systems. Smart grids are not new grids but the evolutionized version of current grids which aims to address the drawbacks of the existing networks. With incorporating advanced metering devices, e.g., phasor measurement units (PMUs) power grids have become more intelligent, reliable and efficient [12] and this give them ability to control the power system in a better way compared to traditional networks. Smart grids need to be managed actively and economically because of certain uncertainties and variability in loads and generations [14]. With the improvement in data mining, analysis, management [15], control and communication capabilities [16], smart grids aim to respond immediately to any incidents in the system [17]. Smart grids can have multiple benefits including achieving better efficiency, increasing the system reliability, incorporating more renewable energy resources, and reduced natural gas emissions [18-20].

Figure1 illustrates the presence of electric vehicles in a smart grid. As it can be seen, the independent system operator (ISO) with sending the communication signals controls the charge and discharge of electric vehicles either at home or charging stations.

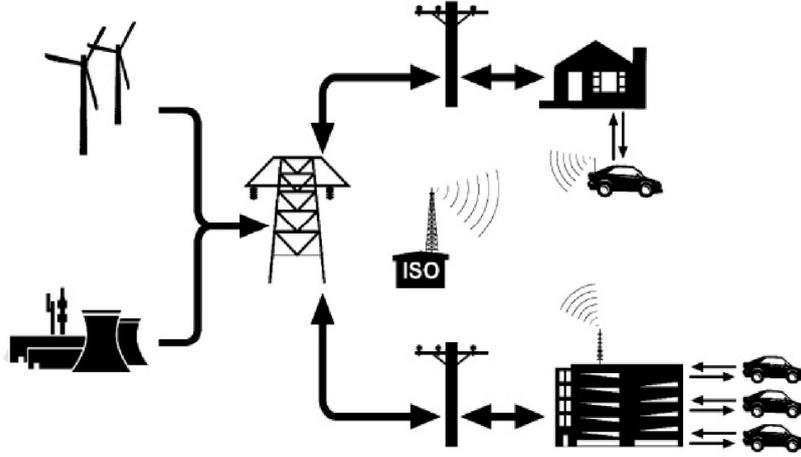


Figure 1. Two-sided communication between electric vehicles and ISO in smart grid.

### 2.2. Objective Function

In this paper, the unit commitment problem is performed by considering the limitation in the line current flows. The objective function is presented in (1).

$$\min \left\{ \sum_{t=1}^T \sum_{i=1}^{Ng} (F_{c,i}(P_{i,t}) \cdot I_{i,t} + SU_{i,t}) + SD_{i,t} + \sum_{t=1}^T \sum_{v=1}^{Nv} C_{v,t} \right\} \quad (1)$$

This objective function aims at minimizing the overall cost of generating units and calculating the optimal value for charge and discharge of EVs. The cost function of the generating unit is usually considered a polynomial function as in (2).

$$F_{c,i}(P_i(t)) = a_i \cdot P_i^2(t) + b_i \cdot P_i(t) + c_i \quad (2)$$

Using this equation in the optimization problem leads to a non-linear problem. A piece-wise linear model is considered for this non-linear function to linearize the function. Therefore, The new model can be presented as

$$\begin{aligned} F_{c,i}(P_{i,t}, I_{i,t}) &= F_{c,i}(P_i^{min}) \cdot I_{i,t} + \sum_{k=1}^{kk} \rho_{i,t}^k P_{i,t}^k \\ 0 &\leq P_{i,t}^k \leq P_i^{k,max} \quad \forall k, \forall i, \forall t \\ P_{i,t} &= P_i^{min} I_{i,t} + \sum_{k=1}^{kk} P_{i,t}^k \end{aligned} \quad (3)$$



Table 2. EV Fleet Trip Specifics.

Fleet	No. of EV	First Trip				Second Trip				Energy per hr (MW)
		Departure		Arrival		Departure		Arrival		
		Time	Bus	Time	Bus	Time	Bus	Time	Bus	
1	3400	6	5	8	1	17	1	19	5	7.25
2	2000	7	4	8	2	16	2	17	4	9
3	1000	5	4	7	2	16	2	18	4	2.25
4	1600	5	6	6	3	17	3	18	6	7.2
5	2000	7	5	9	3	18	3	20	5	4.5

Each EV in the fleet drives 12000 miles annually and 33 miles daily on average [24, 25]. On average, the daily consumed energy and driven distance are 9kW/day and 3.65 miles/kWh, respectively [26]. In this paper, it is assumed that the consumed energy in the departure and arrival routes are the same.

To solve the unit commitment problem, the mixed-integer linear programming (MILP) technique is deployed, and the simulations are performed in GAMS software which is a very powerful tool for dealing with optimization problems. To solve the problem, the CPLEX method which is one of the efficient techniques for solving the MIP is used [27].

### 3. Result and Discussion

Using the mentioned method, the problem is solved in three modes and. 1) without considering of the EVs, 2) with considering the EVs but assuming they are not moving, and 3) with considering the EVs and assuming they are moving. The results are shown in Table 3. As it can be seen the operation

cost for the third case is \$134345.

Table 3. Operating cost comparison.

Without EVs	\$136335
With EVs and not moving	\$130869
With EVs and moving	\$134345

Table 4 shows the charge and discharge of EV fleet during 24 hours. It is noticeable from the table that during hours 1 and 12 where there is no peak load, the batteries are charged. On the other hand, during hours 13 and 24 where the network faces the peak load, most of the fleets are in the discharge mode (the negative power means charging, and positive power means discharging). If it is assumed that the EVs are not moving during the day and are always connected to grid in the charging parking, then the operation cost reduces to \$130869. This is because in this case no energy is consumed for driving the EV. Table 3 shows that the presence of EVs in the grid reduces the operation costs.

Table 4. The amount of charge and discharge power of the EV fleet per hour in terms of megawatt in 24 hours.

Fleet	Hours between (1-12)					
	1	2	3	4	5	6
	7	8	9	10	11	12
1	0	0	0	-8.27	-9.72	0
	0	-9.72	0	-3.55	-9.72	-9.72
2	0	0	0	0	0	0
	0	0	0	0	-5.71	-11.1
3	0	0	0	0	0	0
	0	0	0	0	-3.93	-2.85
4	-2.49	-4.98	-8.97	-9.14	0	-6.67
	-9.14	-4.57	-3.74	0	0	0
5	-5.71	-5.71	-8.87	-8.41	-11.43	-11.43
	0	0	-5.71	-3.98	0	3.05
	Hours between (13-24)					
Fleet	13	14	15	16	17	18
	19	20	21	22	23	24
1	-9.72	0	-9.72	-9.72	0	-9.72
	8.16	7.02	7.02	7.02	7.02	1.04
2	-8.21	-10.24	-11.43	0	0	0
	4.13	4.13	4.13	1.42	4.13	0
3	-5.11	-2.85	-11.43	0	0	0
	2.06	2.06	2.06	0	0	0
4	0	0	0	0	0	3.30
	8.22	6.60	4.43	1.99	3.30	0
5	4.74	4.32	1.77	2.65	4.21	0
	0	5.14	4.13	3.06	0.97	0

With the closer look at the charging and discharging process at Table 4, it can be seen that when the EVs are located at bus 6 and then move to bus 3 at 5 o'clock, they are charging between hours 1 and 9 (except hour 5), which is due to the low local

marginal price at these buses during these hours. In addition, it can be seen from Figure 3 that bus 6 has the highest of its local marginal price during the hours 18 and 24. Therefore, when the EVs of fleet 4 go this bus, they give energy to the grid

during these hours. Moreover, Figure 3 shows that bus 3 and bus 2 have the maximum, and minimum amount of local marginal price (LMP) during hours 10 and 17. Consequently according to tables 2 and 4 when EVs are connected to the grid

at bus 3 (fleets 4 and 5) during these hours, they are not charging and prefer to sell power to the grid and when EVs are connected to bus 2 (fleets 2 and 3), they do not give energy to the grid.

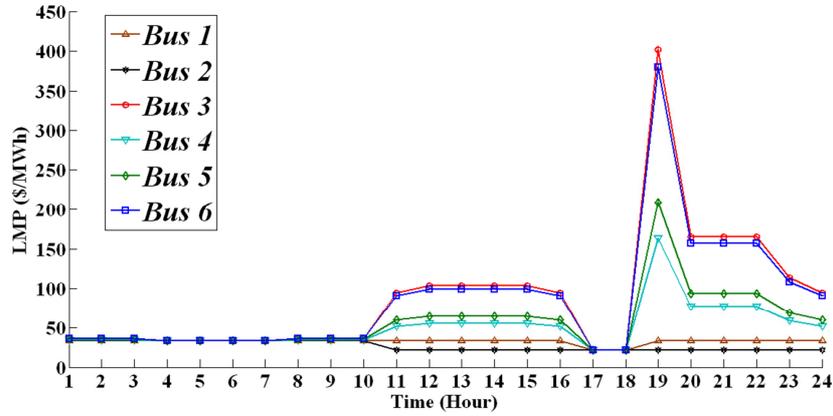


Figure 3. LMP of the network without the presence of EVs.

Figure 4 shows that with the presence of EVs in the network and considering that they are moving, during hours 18 and 24 which are the peak load hours, the LMP decreases significantly.

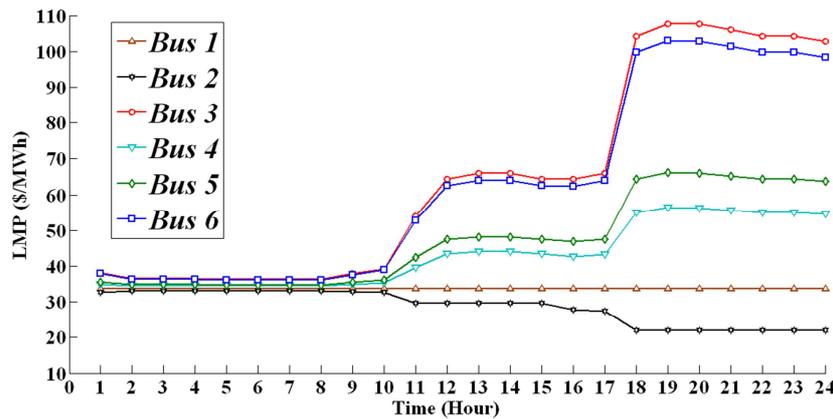


Figure 4. LMP of the network considering the presence of moving EVs.

Figure 5 shows the LMP of the network with the presence of EVs and considering that they are not moving. This figure shows that LMPs of buses 3, 4, 5, and six from hour 10 have reached their maximum values. While according to Figure 4 from hour 18 the LMP at this buses have reached their maximum values. This obviously shows that moving the EVs in the grid reduces line congestion and consequently reduces the LMPs of these buses from hours 10 and 18.

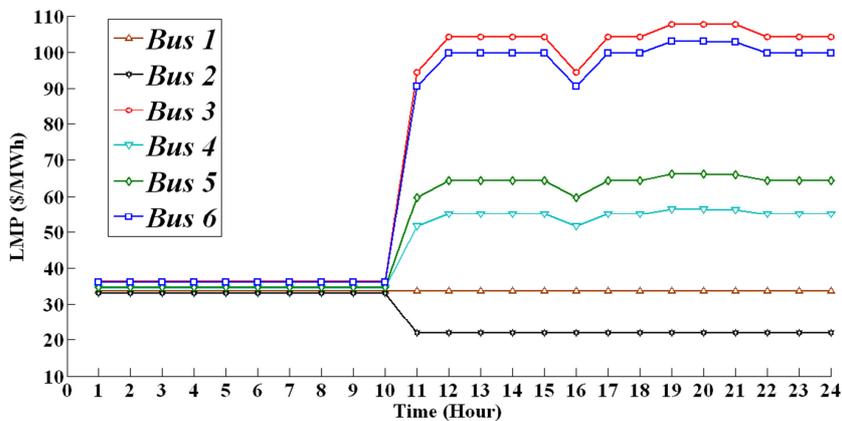


Figure 5. LMP of the network considering the presence of not moving EVs.

To investigate the effect of the line congestion on the system security, we decrease the capacity factor of line 3. As it can be seen from Figure 6. When the EV fleet is not in the network, the network can maintain stable only 0.7 of the line 3 capacity factor. While, when the EVs are present in the network, they can maintain the system security up to 0.3 of

line 3 capacity factor and when the capacity of the line 3 is reduced to 0.3, just the movement of EVs can provide system security. Moreover when EVs are present in the network while the congestion of lines increases, the movement of EVs creates less operation cost compared with they are not moving.

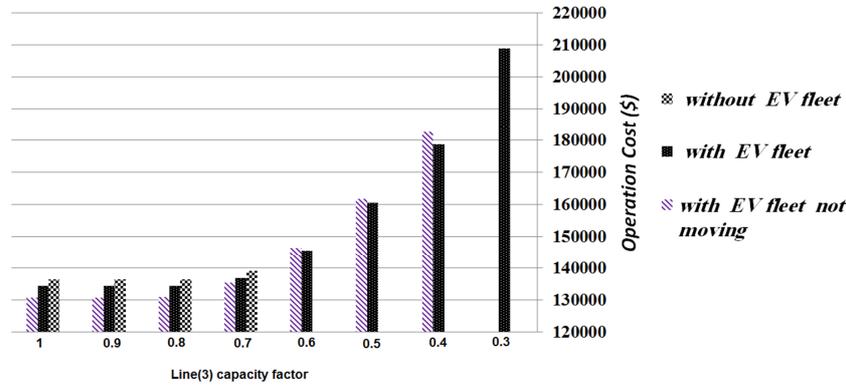


Figure 6. System security with an increase in the line congestion.

Figure 7 shows the sensitivity of the operation cost concerning the number of EVs. It can be seen from the figure that if the number of EVs become 0.7 of the anticipated number, then the operation cost becomes minimum. Also, with the increase in the number EVs from 0.2 to 0.8 of the current number, the operation cost of the thermal unit decreases. However, after 0.8, the operation cost increases. This is because, with the increase in the number of EVs, the charge/discharge

costs of batteries, and therefore, the power generation cost of the thermal units increase. Moreover, this figure shows that with the increase in the number of the EVs, the operation cost of EVs increase. However, after 0.8 the curve tends to become a constant. This is because with the increase in the number of EVs the charge/discharge cost of batteries increase and therefore, the operator prefers to use the thermal units instead of using the extra power provided by EVs.

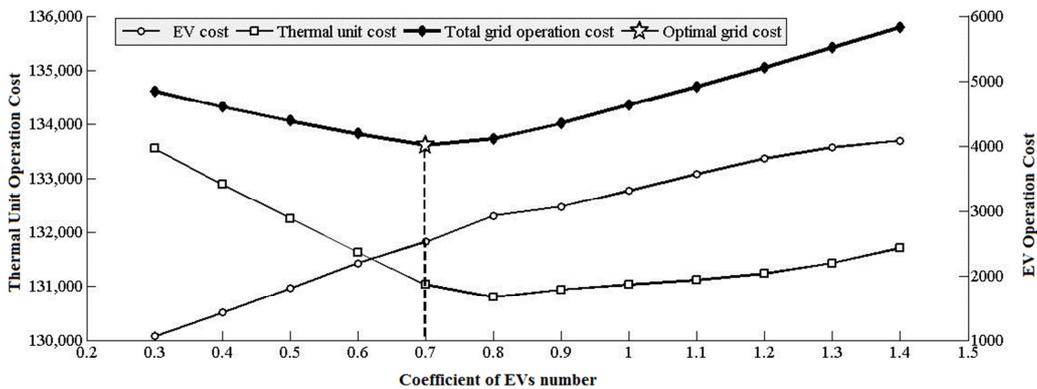


Figure 7. The sensitivity of the operation cost concerning the number of EVs.

Table 5. Status Of Charging (SOC) of the EV fleets in 24 hours in percent.

Fleet	Hours between (1-12)					
	1	2	3	4	5	6
1	20	20	20	30.70	43.27	31.63
	20	32.57	32.57	37.16	49.73	62.30
2	36.42	36.42	36.42	36.42	36.42	36.42
	20	20	20	20	28.86	46.18
3	36.42	36.42	36.42	36.42	28.21	20
	20	20	20	20	32.21	41.07
4	24.84	34.50	51.90	69.64	53.21	66.15
	83.88	92.75	100	100	100	100
5	28.86	37.73	51.49	64.54	82.27	100
	91.79	83.58	92.44	98.63	98.63	93.05

Fleet	Hours between (1-12)					
	1	2	3	4	5	6
	7	8	9	10	11	12
	Hours between (13-24)					
Fleet	13	14	15	16	17	18
	19	20	21	22	23	24
1	74.78	74.78	87.43	100	88.37	76.73
	64.31	53.63	42.95	32.27	21.58	20
2	58.91	75.42	93.15	76.42	76.72	69.18
	61.65	54.11	46.57	43.96	36.42	36.42
3	56.93	65.79	75.45	67.24	59.03	59.03
	51.49	43.96	36.42	36.42	36.42	36.42
4	100	100	100	100	83.58	76.04
	57.27	42.20	32.09	27.54	20	20
5	84.38	76.50	73.26	68.41	60.72	52.51
	44.30	34.90	27.36	21.77	20	20

Table 5 shows that how the smart grid controls status of charging (SOC) of the EVs battery in 24 hours, in order to operate the network at a minimum cost, and also provide ample energy for the EVs in daily trips.

### 4. Conclusion

In this paper, the unit commitment problem with considering the electric vehicles (EVs) with V2G technology and security constraints is solved. In this paper, the EVs are modeled in large scale in a smart grid. The model is linearized and is implemented with MIP in the GAMS software and is

solved with CPLEX method. The effects of the EVs on the operation cost and power generation of thermal units are investigated. Furthermore, the impacts of displacing the EVs on the system security and local marginal price are studied. The results show that with the presence of the EVs in the peak loads hours and injection of the power to grid, there is no need for expensive units to generate power. The moving ability of the EVs, makes them to serve as the transmission lines and transmit power from one bus to another and reducing the line congestion and consequently, decreasing the LMP. Furthermore, due to the energy saving ability of the EVs and generating power, the system security increases.

### Nomenclature

Cost function of $i^{th}$ unit	$F_{c,i}(\cdot)$
Power generation of $i^{th}$ unit at time t	$P_{i,t}$
charge power / discharge power of $v^{th}$ fleet at time t	$P_{dc,v,t}/P_{c,v,t}$
The operating cost of electrical vehicle fleets	$C_{(\cdot)}$
The available energy in the batteries of $v^{th}$ fleet at time t	$E_{v,t}^{(\cdot)}$
Min / Max energy stored in the battery of the $v^{th}$ fleet	$E_v^{max}/E_v^{min}$
Minimum / Maximum charge rate of the $v^{th}$ fleet	$p_{c,v}^{max}/P_{c,v}^{min}$
Minimum / Maximum discharge rate of the $v^{th}$ fleet	$p_{dc,v}^{max}/P_{dc,v}^{min}$
Charging mode of $v^{th}$ fleet	$I_{c,v,t}$
Discharging mode of $v^{th}$ fleet	$I_{dc,v,t}$
Idle mode of $v^{th}$ fleet	$I_{i,v,t}$
On / Off mode of $i^{th}$ unit at time t	$I_{i,t}$
Total load of network	$P_{D,(\cdot)}$
Total number of buses	$NB$
The number of thermal units located on the $b^{th}$ bus	$NG$
The total number of transmission lines	$b$
The slope of the cost function for k-piece	$NL$
the slope of the m-part of the linear charging and discharging curve of the $v^{th}$ fleet	$\rho_{i,t}^k$
the linear charging and discharge curve of the $v^{th}$ fleet at time t and in mth part	$b_{m,v}$
Net energy delivered to the network	$P_{m,v,t}$
The number of transmission lines located at the $b^{th}$ bus	$E_{v,t}^{net}$
The amount of energy consumed by each fleet per hour of movement	$NL_b$
The minimum output power of $i^{th}$ unit	$DR_{v,t}$
Maximum output power of $i^{th}$ unit	$p_t^{min}$
	$p_t^{max}$

The startup cost of $i^{\text{th}}$ unit at t-time	$SU_{i,t}$
The shutdown cost of the $i^{\text{th}}$ unit at time t	$SD_{i,t}$
The reactance of line l	$X_l$
The angle of each bus	$\theta_{(.)}$
The maximum transmission capacity of line l	$PL_l^{\text{max}}$
The state of connection to the network of $v^{\text{th}}$ fleet at time t	$N_{v,t}$
Charging cycle efficiency of the $v^{\text{th}}$ fleet	$\eta_v$

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