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# Statistical evaluation of indicators of diagnostic test performance

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**Abstract:** Diagnostic accuracy relates to the ability of a test to discriminate between the target condition and health. This discriminative potential can be quantified by the measures of diagnostic accuracy such as sensitivity and specificity, predictive values, likelihood ratios, error rates, the area under the ROC curve, Youden's index and diagnostic odds ratio. Different measures of diagnostic accuracy relate to the different aspects of diagnostic procedure: while some measures are used to assess the discriminative property of the test, others are used to assess its predictive ability. Measures of diagnostic accuracy are not fixed indicators of a test performance, some are very sensitive to the disease prevalence, while others to the spectrum and definition of the disease. Furthermore, measures of diagnostic accuracy are extremely sensitive to the design of the study. Studies not meeting strict methodological standards usually over- or under-estimate the indicators of test performance as well as they limit the applicability of the results of the study. STARD initiative was a very important step toward the improvement of the quality of reporting of studies of diagnostic accuracy. STARD statement should be included into the Instructions to authors by scientific journals and authors should be encouraged to use the checklist whenever reporting their studies on diagnostic accuracy. Such efforts could make a substantial difference in the quality of reporting of studies of diagnostic accuracy and serve to provide the best possible evidence to the best for the patient care. This brief review outlines some basic definitions, formulas and characteristics of the measures of diagnostic accuracy.

**Keywords:** Diagnostic Accuracy, Sensitivity, Specificity, Likelihood Ratio, DOR, AUC, Predictive Values

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## 1. Introduction

There is no single statistic that can adequately represent the agreement between a diagnostic test and a reference standard. Many different statistics have a part to play in the analysis of such studies. This discriminative ability can be quantified by the measures of diagnostic accuracy: Sensitivity, Specificity, Receiver operating characteristic curve (ROC curve), Likelihood ratio (LR) for positive test, Likelihood ratio (LR) for negative test, Odds ratio (OR), Positive predictive value (PPV), Youden's index, Negative predictive value (NPV), Error rates and Confidence interval. Diagnostic accuracy of any diagnostic procedure or a test gives us an answer to the following question: "How well this test discriminates between certain two conditions of interest (health and disease; two stages of a disease etc.)?". Different measures of diagnostic

accuracy relate to the different aspects of diagnostic procedure. Some measures are used to assess the discriminative property of the test, others are used to assess its predictive ability (Irwig et al, 2002). While discriminative measures are mostly used by health policy decisions, predictive measures are most useful in predicting the probability of a disease in an individual (Raslich et al, 2007). Furthermore, it should be noted that measures of a test performance are not fixed indicators of a test quality and performance. Measures of diagnostic accuracy are very sensitive to the characteristics of the population in which the test accuracy is evaluated. Some measures largely depend on the disease prevalence, while others are highly sensitive to the spectrum of the disease in the studied population. It is therefore of utmost importance to know how to interpret them as well as when and under what conditions to use them.

## 2. Diagnostic Effectiveness

Another global measure of diagnostic accuracy is so called diagnostic accuracy (effectiveness), expressed as a proportion of correctly classified subjects (TP+TN) among all subjects (TP+TN+FP+FN). Diagnostic accuracy is affected by the disease prevalence. With the same sensitivity and specificity, diagnostic accuracy of a particular test increases as the disease prevalence decreases. This data, however, should be handled with care. In fact, this does not mean that the test is better if we apply it in a population with low disease prevalence. It only means that in absolute number the test gives more correctly classified

subjects. This percentage of correctly classified subjects should always be weighed considering other measures of diagnostic accuracy, especially predictive values. Only then a complete assessment of the test contribution and validity could be made.

Consider table 1 below which indicates the test status and disease condition of patient from where some common indicators of test performance will be derived. Some of these indicators are the sensitivity of the test, its specificity, the positive and negative predictive values, Odds ratio, error rates and the positive and negative likelihood ratios (Sackett, 1991).

**Table 1.** Cross –classification of test results by Test status and disease status

(Test status)	Positive ( $B$ )	Negative ( $\bar{B}$ )	Total
Positive ( $A$ )	$A = TP$	$B = FP$	$A+B=TP+FP=P$
Negative ( $\bar{A}$ )	$C = FN$	$D = TN$	$C+D=FN+TN= P'$
Total	$A+C=TP+FN= Q$	$B+D=FP+TN= Q'$	$N= TP+FN+FP+TN$

A frequent application of Bayes' theorem is in evaluating the performance of a diagnostic test intended for use in a screening program. From table 1 above, let  $B$  denote the event that a person has the disease in question;  $\bar{B}$  the event that he does not have the disease; let  $A$  be the event that he gives a positive response to the test; and  $\bar{A}$  the event that he gives a negative response. Let  $P$  be the Prevalence of the disease. Prevalence is the number of cases of a disease that are present in a particular population at a given time (Dohoo et al, 2003). Based on the above table, it is given by  $P = \text{mean}(p_i)$  while  $Q$  is the level of the test given by  $Q = \text{mean}(q_i)$ . But  $P' = 1-P$  and  $Q' = 1-Q$ . From this table 1, TP is true positive, FN is false positive, TN is true negative and FP is false positive while  $N$  is the total number of patients/subject considered. The first step in the calculation of sensitivity and specificity is to make a 2x2 table with groups of subjects divided according to a gold standard or (reference method) in columns, and categories according to test in rows as seen in table 1 above.

## 3. Sensitivity and Specificity

The first step in the calculation of sensitivity and specificity is to make a 2x2 table with groups of subjects divided according to a gold standard or (reference method) in columns, and categories according to test in rows (Table 1.).

Let  $\pi$  and  $\theta$  be sensitivity and specificity of the tests respectively. The results of this trial of the screening test may be represented by the two conditional probabilities  $P(A|B)$  and  $P(\bar{A}|\bar{B})$ . Sensitivity is expressed in percentage and defines the proportion of true positive subjects with the disease in a total group of subjects with the disease ( $TP/TP+FN$ ). Actually, sensitivity is defined as the probability of getting a positive test result in subjects

with the disease ( $T+|B+$ ). Hence, it relates to the potential of a test to recognize subjects with the disease. The sensitivity ( $\pi$ ) given as  $P(A|B)$  is the conditional probability of a positive response given that the person has the disease; the larger is  $P(A|B)$ , the more sensitive is the test. From table 1, conditional probability in terms of sensitivity is also given by

$$P(T = 1 | D = 1) = \Pr(T + | D +) = \frac{TP}{TP + FN} \quad (1)$$

While  $P(\bar{A}|\bar{B})$  is the conditional probability of a negative response given that the person is free of the disease; the smaller is  $P(\bar{A}|\bar{B})$ , the more specific is the test. We can also define that  $1 - \pi = P(T = 0 | D = 1)$ . Specificity is a measure of a diagnostic test accuracy, complementary to sensitivity. It is defined as a proportion of subjects without the disease with negative test result in total of subjects without disease ( $TN/TN+FP$ ). In other words, specificity represents the probability of a negative test result in a subject without the disease ( $T-|B-$ ). Therefore, we can postulate that specificity relates to the aspect of diagnostic accuracy that describes the test ability to recognize subjects without the disease, i.e. to exclude the condition of interest. From table 1 also, specificity is given by

$$P(T = 0 | D = 0) = \Pr(T - | D -) = \frac{TN}{FP + TN} \quad (2)$$

Also  $1 - \theta = P(T = 1 | D = 0)$ . Neither sensitivity nor specificity is not influenced by the disease prevalence, meaning that results from one study could easily be transferred to some other setting with a different prevalence of the disease in the population. Nonetheless, sensitivity and specificity can vary greatly depending on the spectrum

of the disease in the studied group. Worthy of note also is the predictive values which includes the positive predictive values (PPV) and negative predictive values (NPV). Positive predictive value (PPV) defines the probability of having the state/disease of interest in a subject with positive result ( $B+|T+$ ). Therefore PPV represents a proportion of patients with positive test result in total of subjects with positive result ( $TP/TP+FP$ ). PPV is defined as the probability of a positive diagnosis when the test is positive. Therefore, PPV represents a proportion of patients with positive test result in total of subjects with positive result. It is also seen as the ratio of the number of true positives to the total number of positive tests (Staquet et al 1981). In terms of Bayes formula, it is given by

$$PPV = P(D+|T+) = \frac{P(T+|D+)P(D+)}{P(T+)} = (SE.P) / Q = TP / Q \quad (3)$$

where  $Q = TP + FP = \text{level of the test}$

Negative predictive value (NPV) describes the probability of not having a disease in a subject with a negative test result ( $B-|T-$ ). NPV is defined as a proportion of subjects without the disease with a negative test result in total of subjects with negative test results ( $TN/TN+FN$ ). Also the NPV in terms of Bayes formula is the probability of negative diagnosis when the test is negative or the proportion of subjects without the disease with a negative test result in total of subjects with negative test results and it is given by

$$NPV = P(D-|T-) = \frac{P(T-|D-)P(D-)}{P(T-)} = TN / Q' \text{ where } Q' = TN + FN \quad (4)$$

According to the table 1 above for conditional probability, the predictive values are defined mathematically as:

$$PPV = \frac{TP}{TP+FP} = P(D+|T+) \text{ or } P(T+|D+) \quad (5)$$

$$NPV = \frac{TN}{FN+TN} = P(D-|T-) \text{ or } P(T-|D-) \quad (6)$$

Also the two can be defined as  $PPV = \Pr(D=1|T=1)$  and  $NPV = \Pr(D=0|T=0)$ .

Unlike sensitivity and specificity, predictive values are largely dependent on disease prevalence in examined population. Unlike sensitivity and specificity, predictive values are largely dependent on disease prevalence in examined population. Therefore, predictive values from one study should not be transferred to some other setting with a different prevalence of the disease in the population. Prevalence affects PPV and NPV differently. PPV is increasing, while NPV decreases with the increase of the prevalence of the disease in a population. Whereas the

change in PPV is more substantial, NPV is somewhat weaker influenced by the disease prevalence. Therefore, predictive values from one study should not be transferred to some other setting with a different prevalence of the disease in the population. Prevalence affects PPV and NPV differently. PPV is increasing, while NPV decreases with the increase of the prevalence of the disease in a population. Whereas the change in PPV is more substantial, NPV is somewhat weaker influenced by the disease prevalence. It is important to say that there exist error rates to be expected if the test is actually used in a screening program. If a positive result is taken to indicate the presence of the disease, then the false positive rate (FPR) or say  $P_{F+}$  is the proportion of people, among those responding positive, who are actually free of the disease. It can also be denoted as  $P(\bar{B}|A)$ . According to Bayes' theorem and based on the table 1,

$$P_{F+} = P(\bar{B}|A) = P(T=1|D=0) = 1 - \theta = \frac{P(A|\bar{B})P(\bar{B})}{P(A)} = \frac{P(A|\bar{B})(1-P(B))}{P(A)} \quad (7)$$

Since  $P(\bar{B}) = 1 - P(B)$ .

The false negative rate (FNR) or say  $P_{F-}$ , is the proportion of people, among those responding negative on the test, who nevertheless have the disease, or  $P(B|\bar{A})$ . Again by Bayes' theorem,

$$P_{F-} = P(B|\bar{A}) = 1 - \pi = P(T=0|D=1) = \frac{P(\bar{A}|B)P(B)}{P(\bar{A})} = \frac{(1-P(A|B))P(B)}{1-P(A)} \quad (8)$$

Since  $P(\bar{A}|B) = 1 - P(A|B)$  and  $P(\bar{A}) = 1 - P(A)$ .

Looking at the mathematical definitions of FPR and FNR above, one discovers that  $P(A)$  and  $P(B)$  has to be clearly defined so as to make the formulas complete.

## 4. Derivation of the Error Rates Formulas

A perfect diagnostic procedure has the potential to completely discriminate subjects with and without disease. Values of a perfect test which are above the cut-off are always indicating the disease, while the values below the cut-off are always excluding the disease. Unfortunately, such perfect test does not exist in real life and therefore diagnostic procedures can make only partial distinction between subjects with and without disease. Values above the cut-off are not always indicative of a disease since subjects without disease can also sometimes have elevated values. Such elevated values of certain parameter of interest are called false positive values (FP). On the other hand, values below the cut-off are mainly found in subjects without disease. However, some subjects with the disease can have them too. Those values are false negative values (FN). Therefore, the cut-off divides the population of examined subjects with and without disease in four subgroups considering parameter values of interest.

According to table 1 above, we define as follows the following terms:

- 1 true positive (TP) –subjects with the disease with the value of a parameter of interest above the cut-off
- 2 false positive (FP) –subjects without the disease with the value of a parameter of interest above the cut-off
- 3 true negative (TN) –subjects without the disease with the value of a parameter of interest below the cut-off
- 4 false negative (FN) –subjects with the disease with the value of a parameter of interest below the cut-off

Let us consider  $P(A)$  and  $P(B)$  for this evaluation based on table 1 above. If

$$P(A) = \frac{N_A}{N} = \frac{N_{AB} + N_{A\bar{B}}}{N} = \frac{N_{AB}}{N} + \frac{N_{A\bar{B}}}{N} \quad (9)$$

and  $N_A$  indicates the total number of people who test positive, then  $N_{AB}$  denotes the number of people who have the disease and respond positive while  $N_{A\bar{B}}$  denotes the number of people who are free of the disease and respond positive. Multiplying and dividing the first of the two terms on the right-hand side of the above equation by  $N_B$ , the number of people with the disease, we find that

$$\frac{N_{AB}}{N} = \frac{N_{AB}}{N_B} \frac{N_B}{N} = P(A|B)P(B) \quad (10)$$

Similarly, by multiplying and dividing the second term by  $N_{\bar{B}}$ , the number of people without the disease, we find that

$$\frac{N_{A\bar{B}}}{N} = \frac{N_{A\bar{B}}}{N_{\bar{B}}} \frac{N_{\bar{B}}}{N} = P(A|\bar{B})P(\bar{B}) \quad (11)$$

Substituting the expressions from the above last three equations in  $P(A)$  defined above, we find that

$$P(A) = P(A|B)P(B) + P(A|\bar{B})P(\bar{B}) \quad (12)$$

This equation is a special case of the familiar result that an overall rate-  $P(A)$  is a weighted average of specific rates-  $P(A|B)$  and  $P(A|\bar{B})$  -with the weights being the proportions of people in the specific categories  $P(B)$  and  $P(\bar{B})$ . Since  $P(\bar{B}) = 1 - P(B)$ , then the above equation becomes

$$\begin{aligned} P(A) &= P(A|B)P(B) + P(A|\bar{B})(1 - P(B)) \\ &= P(A|\bar{B}) + P(B)(P(A|B) - P(A|\bar{B})) \end{aligned} \quad (13)$$

Substituting this equation in the equation of  $P_{F+}$  above yields an expression for the FPR thus,

$$P_{F+} = \frac{P(A|\bar{B})(1 - P(B))}{P(A|\bar{B}) + P(B)(P(A|B) - P(A|\bar{B}))} \quad (14)$$

Also substituting for  $P(A)$  in the equation of  $P_{F-}$  above yields the expression for the FNR or

$$P_{F-} = \frac{(1 - P(A|B))P(B)}{1 - P(A|\bar{B}) - P(B)(P(A|B) - P(A|\bar{B}))} \quad (15)$$

In conclusion, the two error rates are functions of the proportions  $P(A|B)$  and  $P(A|\bar{B})$  which may be estimated from the results of a trial of the screening test; and of the overall case rate  $P(B)$ , for which an accurate estimate is rarely available.

## 5. Likelihood Ratios

Likelihood ratio is a very useful measure of diagnostic accuracy. It is defined as the ratio of expected test result in subjects with a certain state/disease to the subjects without the disease. From a clinical standpoint, a diagnostic test should give a sense of how more or less likely the disease being tested for is present or not, i.e., does the result of the diagnostic test change probability of the disease being present or not? Likelihood ratios can quantify the change in the probability of disease given the results of a diagnostic test. Likelihood ratios are alternative statistics for summarizing diagnostic accuracy, which have several particularly powerful properties that make them more useful clinically than other statistics (Sackett et al, 2000). Each test result has its own likelihood ratio, which summarizes how many times more (or less) likely patients with the disease are to have that particular result than patients without the disease. More formally, it is the ratio of the probability of the specific test result in people who do have the disease to the probability in people who do not. A likelihood ratio greater than 1 indicates that the test result is associated with the presence of the disease, whereas a likelihood ratio less than 1 indicates that the test result is associated with the absence of disease. The further likelihood ratios are from 1 the stronger the evidence for the presence or absence of disease. Likelihood ratios above 10 and below 0.1 are considered to provide strong evidence to rule in or rule out diagnoses respectively in most circumstances (Jaeschke et al, 2002). In other words, it indicates large, often clinically significant differences. A likelihood ratio of 1 implies that there will be no difference between pretest and posttest probabilities. In other words, the two ratios are equal, such that the test is of no value. Likelihood ratios between 1 and 2 and between 0.5 and 1 indicate small differences (rarely clinically significant). When tests report results as being either positive or negative the two likelihood ratios are called the positive likelihood ratio and the negative likelihood ratio. It is vital to note that sensitivity and specificity are combined into one to have the likelihood ratio (LR). The likelihood ratio is

defined as: “The probability of a subject with the disease having the test result divided by the probability of the subject without the disease having that same test result”(Giard and Hermans,1996).From table 1 above

$$LR = \frac{\text{Probability of result in diseased persons}}{\text{Probability of result in nondiseased persons}} \quad (16)$$

When test results are dichotomized, every test has two likelihood ratios, one corresponding to a positive test and that of negative test. Positive test likelihood ratio ( $LR^+$ ) tells us how much more likely the positive test result is to occur in subjects with the disease compared to those without the disease. It is usually higher than 1 because it is more likely that the positive test result will occur in subjects with the disease than in subject without the disease.  $LR^+$  is the best indicator for ruling-in diagnosis. The higher the  $LR^+$  the test is more indicative of a disease. Good diagnostic tests have  $LR^+ > 10$  and their positive result has a significant contribution to the diagnosis.  $LR^+$  can be simply calculated according to the following formulas:

$$LR^+ = \frac{\text{Probability that test is positive in diseased persons}}{\text{Probability that test is positive in non - diseased persons}} \quad (17)$$

$$LR^+ = \frac{\text{Sensitivity}}{1 - \text{Specificity}} = \frac{\text{Pr}(T^+|D^+)}{\text{Pr}(T^+|D^-)} = \frac{TP / TP + FN}{FP / FP + TN}$$

Likelihood ratio for negative test result ( $LR^-$ ) represents the ratio of the probability that a negative result will occur in subjects with the disease to the probability that the same result will occur in subjects without the disease. Therefore,  $LR^-$  tells us how much less likely the negative test result is to occur in a patient than in a subject without disease.  $LR^-$  is usually less than 1 because it is less likely that negative test result occurs in subjects with than in subjects without disease.  $LR^-$  is calculated according to the following formulas:

$$LR^- = \frac{\text{Probability that test is negative in diseased persons}}{\text{Probability that test is negative in non - diseased persons}} \quad (18)$$

$$= \frac{1 - \text{Sensitivity}}{\text{Specificity}} = \frac{\text{Pr}(T^-|D^+)}{\text{Pr}(T^-|D^-)} = \frac{FN / TP + FN}{TN / FP + TN}$$

$LR^-$  is a good indicator for ruling-out the diagnosis. Good diagnostic tests have  $LR^- < 0.1$ . The lower the  $LR^-$  the more significant contribution of the test is in ruling-out, i.e. in lowering the posterior probability of the subject having the disease. Since both specificity and sensitivity are used to calculate the likelihood ratio, it is clear that neither  $LR^+$  nor  $LR^-$  depend on the disease prevalence in examined groups. Consequently, the likelihood ratios from one study are applicable to some other clinical setting, as long as the definition of the disease is not changed. If the way of defining the disease varies, none of the calculated measures will apply in some other clinical context. Meanwhile, it is also important to define mathematically the following terms as it relates to table 1 above.

$$\text{Pretest probability(Prevalence)} = \frac{\text{Pretest probability}}{1 - \text{Pretest probability}}$$

$$\text{Pretest probability} = \frac{TP + FN}{TP + FP + TN + FN} \quad (19)$$

$$\text{Pretest Odds} = \frac{\text{Prevalence}}{1 - \text{Prevalence}} = \frac{TP + FN}{FP + TN} \quad (20)$$

$$\text{Posttest probability} = \frac{\text{Post test Odds}}{1 + \text{post test odds}} \quad (21)$$

$$\text{Posttest Odds} = \text{Pretest Odds} \times \text{Likelihood ratio} \quad (22)$$

$LR$  directly links the pre-test and post-test probability of a disease in a specific patient (Deeks and Altman,2004). Simplified,  $LR$  tells us how many times more likely particular test result is in subjects with the disease than in those without disease. Likelihood ratios provide an estimation of whether there will be significant change in pretest to posttest probability of a disease given the test result, and thus can be used to make quick estimates of the usefulness of contemplated diagnostic tests in particular situations. The simplest method for calculating posttest probability from pretest probability and likelihood ratios is to use a nomogram. The clinician places a straightedge through the points that represent the pretest probability and the likelihood ratio and then reads the posttest probability where the straightedge crosses the posttest probability line. A more formal way of calculating posttest probabilities uses the likelihood ratio as follows: Pretest odds  $\times$  Likelihood ratio=Posttest odds.

## 6. Odds Ratio

The Odds ratio or diagnostic odds ratio is the probability of the presence of a disease of a specific disease divided by the probability of its absence. Diagnostic odds ratio is also one global measure for diagnostic accuracy, used for general estimation of discriminative power of diagnostic procedures and also for the comparison of diagnostic accuracies between two or more diagnostic tests. DOR of a test is the ratio of the odds of positivity in subjects with disease relative to the odds in subjects without disease (Glas et al,2003). It is calculated according to the formula:  $DOR = (TP/FN)/(FP/TN)$ . DOR depends significantly on the sensitivity and specificity of a test. A test with high specificity and sensitivity with low rate of false positives and false negatives has high DOR. With the same sensitivity of the test, DOR increases with the increase of the test specificity. For example, a test with sensitivity  $> 90\%$  and specificity of  $99\%$  has a DOR greater than 500. The Odds ratio reflects the prevalence of the disease in a population. For example, the odds are 1:4 for finding a disease in a population with a 20% probability of occurrence (prevalence).Also odds of 3:1 in favor of the first outcome means that the first outcome occurs 3 times for each single occurrence of the second outcome. Similarly, odds of 5:2 means that the first outcome occurs 5 times for each 2 occurrences of the second outcome. To use this formulation above, probabilities must be converted to odds,

where the odds of having a disease are expressed as the chance of having the disease divided by the chance of not having the disease.

Recall that

$$O d d = \frac{P r o b a b i l i t y}{1 - P r o b a b i l i t y} \quad (23)$$

$$P r o b a b i l i t y = \frac{O d d s}{1 + o d d s} \text{ and } P r o b a b i l i t y = \frac{A}{A + B} \quad (24)$$

when odds are expressed as a:b. To estimate the potential benefit of a diagnostic test, the clinician first estimates the pretest odds of disease given all available clinical information and then multiplies the pretest odds by the positive and negative likelihood ratios. The results are the posttest odds, or the odds that the patient has the disease if the test is positive or negative. To obtain the posttest probability, the odds are converted to a probability as seen above. Meanwhile, odds ratio is a measure of effect size, describing the strength of association or non independence between two binary data values (Cornfield, 1964; Mosteller, 1968; Edwards, 1963). It is used as a descriptive statistic, and plays an important role in logistic regression. Unlike other measures of association for paired binary data such as the relative risk, the odds ratio treats the two variables being compared symmetrically, and can be estimated using some types of non-random samples.

## 7. Derivation of Odds Ratio Formular For Ad/Bc

From table 1 above where we have the test result status and disease status categorized/classified into A,B,C and D. We shall have the following:

$$Odds \text{ of exposure with disease} = \frac{\text{Probability of exposure in those with disease}}{1 - \text{Probability of exposure in those with disease}} \quad (25)$$

$$\text{But, Prob of exposure in those with the disease} = \frac{A}{A + C}$$

Therefore,

$$\begin{aligned} Odds \text{ of exposure with the disease} &= \frac{A}{A + C} / 1 - \frac{A}{A + C} \\ &= \frac{A}{A + C} / \frac{C}{A + C} = \frac{A}{C} \end{aligned} \quad (26)$$

Similarly,

$$Odds \text{ of exposure without the disease} = \frac{\text{Prob of exposure without disease}}{1 - \text{Prob of exposure without disease}} \quad (27)$$

But,

$$P r o b a b i l i t y \text{ of exposure without disease} = \frac{B}{B + D}$$

$$\begin{aligned} odds \text{ of exposure without the disease} &= \frac{B}{B + D} / 1 - \frac{B}{B + D} \\ &= \frac{B}{B + D} / \frac{D}{B + D} = \frac{B}{D} \end{aligned} \quad (28)$$

$$\text{Since, } 1 - \frac{B}{B + D} = \frac{B + D - B}{B + D} = \frac{D}{B + D},$$

Based on the above contingency table, the odds ratio is interpreted as

$$Odds \text{ ratio} = \frac{Odds \text{ of test result with disease}}{Odds \text{ of same result without disease}} \quad (29)$$

or

$$Odds \text{ ratio} = \frac{Odds \text{ of exposure in those with the disease}}{Odds \text{ of exposure in those without the disease}}$$

$$O d d s ( D + ) = \frac{P r o b a b i l i t y ( D + )}{1 - P r o b a b i l i t y ( D + )} \quad (30)$$

where

$$P r ( D + ) = \frac{O d d s ( D + )}{1 + O d d s ( D + )} \quad (31)$$

In general,

$$O d d s \text{ ratio} = \frac{(A / C)}{(B / D)} = A D / B C \quad (32)$$

## 8. Definition of Odds Ratio in Terms of Group-Wise Odds

The odds ratio is the ratio of the odds of an event occurring in one group to the odds of it occurring in another group. The term is also used to refer to sample-based estimates of this ratio. This group in case of this study is a dichotomous classification. If the probabilities of the event in each of the groups are  $p_1$  (first group) and  $p_2$  (second group), then the odds ratio is:

$$\frac{p_1 / (1 - p_1)}{p_2 / (1 - p_2)} = \frac{p_1 / q_1}{p_2 / q_2} = \frac{p_1 q_2}{p_2 q_1} = \frac{n_{11} / n_{12}}{n_{21} / n_{22}} = \frac{n_{11} n_{22}}{n_{21} n_{12}} \quad (33)$$

where  $q_x = 1 - p_x$ . This is the odds ratio for comparing two proportions. According to Glas et al (2003), OR is based on likelihood and it is given by

$$\text{Diagnostic odds ratio} = \frac{\text{likelihood ratio} +}{\text{likelihood ratio ratio} -} \quad (34)$$

It is vital to note the following points about OR. OR ranges from 0 to infinity with higher values indicating better discriminating test performance. A value of 1 means that a test does not discriminate between patients with the disorder and those without it. That is it shows no difference in risk of group 1 compared to 2. In other words, an odds ratio of 1 indicates that the condition or event under study is equally likely to occur in both groups. The DOR does not depend on the prevalence of the disease (Glas et al, 2003). It tends to be skewed (not symmetric). If  $OR > 1$ , it indicates an increased risk of group 1 compared to 2. This means that an odds ratio greater than 1 indicates that the condition or event is more likely to occur in the first group. If OR is less than 1 it indicates that the condition or event is less likely to occur in the first group meaning that it shows lower risk ("protective") in risk of group 1 compared to 2. The odds ratio must be nonnegative if it is defined. It is undefined if  $p_2 q_1$  equals zero.

## 9. Confidence Intervals

The p values the authors often cite when reporting their results gives a sense of how likely the results reported are due to chance. However, p values do not allow us to make inferences about the precision of the estimates, which is extremely important in evaluating test characteristics. Reporting a range of plausible results, also known as confidence intervals, is more useful. Confidence intervals (CIs) are a measure of how precise an estimate is. The range or width of a confidence interval is primarily determined by two parameters; the number of observations in the study and how widely spread the data are (usually expressed as the standard deviation). The fewer the observations or the greater the data spread, the wider the confidence interval and the greater the uncertainty about the precision of the reported estimate.

## 10. Receiver Operating Characteristic Curve

ROC (Receiver Operating Characteristic) analysis is being used as a method for evaluation and comparison of classifiers (Ferri et al, 2002). The ROC gives complete description of classification accuracy as given by the area under the ROC curve. The ROC curve originates from signal detection theory (Hosmer and Lemeshow, 2000); the curve shows how the receiver operates the existence of signal in the presence of noise. The ROC curve plots the probability of detecting true signal (sensitivity) and false signal ( $1 - \text{specificity}$ ) for an entire range of possible cut points. The sensitivity and specificity of a classifier also depend on the definition of the cut-off point for the probability of predicted classes. A ROC curve demonstrates the trade-off between true positive rate and false positive rate in binary classification problems. To draw a ROC curve, the true positive rate (TPR) and the false positive rate (FPR) are needed. TPR determines the performance of a classifier or a diagnostic test in classifying positive cases correctly among all positive samples available during the test. FPR, on the other hand, defines how many incorrect positive results, which are actually negative, there are among all negative samples available during the test. Because TPR is equivalent to sensitivity and FPR is equal to ( $1 - \text{specificity}$ ), the ROC graph is sometimes called the sensitivity vs. ( $1 - \text{specificity}$ ) plot. The area under the ROC curve has become a particularly important measure for evaluating classifiers' performance because it is the average sensitivity over all possible specificities (Bradley 1997). The larger the area, the better the classifier performs. If the area is 1.0, the classifier achieves both 100% sensitivity and 100% specificity. If the area is 0.5, then we have 50% sensitivity and 50% specificity, which is no better than flipping a coin. This single criterion can be compared for measuring the performance of different classifiers analyzing a dataset. (Hanley, 1982; Bamber, 1975). After a

classifier has been made, it is also useful to measure its calibration. Calibration evaluates the degree of correspondence between the estimated probabilities of a specific outcome resulting from a classifier and the outcomes predicted by domain experts. This can then be tested using goodness-of-fit statistics. This test examines the difference between the observed frequency and the expected frequency for groups of patients and can be used to determine if the classifier provides a good fit for the data. If the p-value is large, then the classifier is well calibrated and fits the data well. If the p-value is small, then the classifier is not well calibrated. There is a pair of diagnostic sensitivity and specificity values for every individual cut-off. To construct a ROC graph, we plot these pairs of values on the graph with the  $1 - \text{specificity}$  on the x-axis and sensitivity on the y-axis. Receiver operating characteristic curve analysis is often used to help determine the cut-off point to optimize sensitivity and specificity. An ROC curve is a graphical representation of the trade off between the false negative and false positive rates for every possible cut-off value (Zweig and Campbell, 1993). Alternatively, the ROC curve is the representation of the trade off between sensitivity and specificity. In other words, the ability of a test using a specific analytic concentration, to discriminate disease from non-disease can be graphically portrayed by use of ROC curve analysis. A graph can be generated in which the sensitivity and specificity are determined for each data point obtained in the study. These are graphed with sensitivity of each data point on the y-axis and the corresponding  $1 - \text{specificity}$  for each data point on the x-axis. Precisely, we plot these pairs of values on the graph with the  $1 - \text{specificity}$  on the x-axis and sensitivity on the y-axis. (Note: the ratio of the y-axis/x-axis is the likelihood ratio positive or the graph of true positives and false positives respectively). For the ideal test, the plot would rise from 0 and go straight up to 1.00 and then a horizontal line along the 1.00 sensitivity line. This would be where there is no overlap in the data points and sensitivity and specificity would both be 100% in the left hand corner (Zweig and Campbell, 1993). This rarely occurs and more commonly a curvilinear plot is observed. The greater the area under the curve, the more discriminatory (the ability of the test to correctly classify those with and without the disease) the test is, ideally, the area under a curve of 1.00 is a perfectly discriminatory test and a curve that follows the diagonal line in the graph has an area under the curve 0.5 which corresponds to the test being no better than flipping a coin (Zweig and Campbell, 1993). The shape of a ROC curve and the area under the curve (AUC) helps us estimate how high is the discriminative power of a test. The closer the curve is located to upper-left hand corner and the larger the area under the curve, the better the test is at discriminating between diseased and non-diseased. The area under the curve can have any value between 0 and 1 and it is a good indicator of the goodness of the test. A perfect diagnostic

test has an AUC 1.0. whereas a non-discrimination test has an area 0.5. The larger the area under the curve, the better the diagnostic test in discriminating those with and without disease (Zweig and Campbell, 1993). Many statistical programs can generate a table of the values in the graph and calculate sensitivity, specificity, LP+, LP-, and proportion or percent correctly identified for each data point. Cut-off points are not necessarily chosen to optimize the number of patients correctly categorized. One can select different cut-off points to optimize sensitivity or specificity. For example, when a screening test is used to look for a serious disease that if missed could result in serious harm to the patient, the sensitivity of that test should be optimized. Conversely, in situations where therapy could be extremely harmful if given to a patient without the disease, one would choose a cut-off point that optimizes specificity. In general, when optimizing one test characteristic, the other gets worse and vice versa. For example, when improving sensitivity, specificity decreases and when improving specificity, sensitivity decreases. The area under the ROC curve can also be used statistically to compare the discriminating ability between two diagnostic tests (Zweig and Campbell, 1993). We can say that the relationship between the area under the ROC curve (AUC) and diagnostic accuracy can be seen in the table below :

**Table 2.1.** Relationship between the area under the ROC curve (AUC) and diagnostic accuracy

Area	Diagnostic Accuracy
0.9-1.0	Excellent
0.8-0.9	Very good
0.7-0.8	Good
0.6-0.7	Sufficient
0.5-0.6	Bad
< 0.5	Test not useful

AUC is a global measure of diagnostic accuracy. It tells us nothing about individual parameters, such as sensitivity and specificity. Out of two tests with identical or similar AUC, one can have significantly higher sensitivity, whereas the other significantly higher specificity. Furthermore, data on AUC state nothing about predicative values and about the contribution of the test in ruling-in and ruling-out a diagnosis. Global measures are there for general assessment and for comparison of two or more diagnostic tests. By the comparison of areas under the two ROC curves we can estimate which one of two tests is more suitable for distinguishing health from disease or any other two conditions of interest. It should be pointed that this comparison should not be based on visual nor intuitive evaluation (Obuchowski *et al.*, 2004). For this purpose we use statistic tests which evaluate the statistical significance of estimated difference between two AUC, with previously defined level of statistical significance (P).

## 11. Youden's Index

Youden's index is one of the oldest measures for diagnostic accuracy (Youden, 1950). It is also a global measure of a test performance, used for the evaluation of overall discriminative power of a diagnostic procedure and for comparison of this test with other tests. Youden's index is calculated by deducting 1 from the sum of test's sensitivity and specificity expressed not as percentage but as a part of a whole number:  $(\text{sensitivity} + \text{specificity}) - 1$ . For a test with poor diagnostic accuracy, Youden's index equals 0, and in a perfect test Youden's index equals 1. Youden's index is not sensitive for differences in the sensitivity and specificity of the test, which is its main disadvantage. Namely, a test with sensitivity 0.9 and specificity 0.4 has the same Youden's index (0.3) as a test with sensitivity 0.6 and specificity 0.7. It is absolutely clear that those tests are not of comparable diagnostic accuracy. If one is to assess the discriminative power of a test solely based on Youden's index it could be mistakenly concluded that these two tests are equally effective. Youden's index is not affected by the disease prevalence, but it is affected by the spectrum of the disease, as are also sensitivity, specificity, likelihood ratios and DOR.

## 12. Design of Diagnostic Accuracy Studies

Measures of diagnostic accuracy are extremely sensitive to the design of the study. Studies suffering from some major methodological shortcomings can severely over- or under-estimate the indicators of test performance as well as they can severely limit the possible applicability of the results of the study. The effect of the design of the study to the bias and variation in the estimates of diagnostic accuracy can be quantified (Rutjes *et al.*, 2006). STARD initiative published in 2003 was a very important step toward the improvement of the quality of reporting of studies of diagnostic accuracy (Bossuyt *et al.*, 2003a; Bossuyt *et al.*, 2003b). According to some authors, the quality of reporting of diagnostic accuracy studies did not significantly improve after the publication of the STARD statement (Wilczynski, 2008 and Bossuyt, 2008), whereas some others hold that the overall quality of reporting has at least slightly improved (Smidt *et al.*, 2006), but there is still some room for potential improvement (Bossuyt, 2006 and Bossuyt, 2004). Editors of scientific journals are encouraged to include the STARD statement into the Journal Instructions to authors and to oblige their authors to use the checklist when reporting their studies on diagnostic accuracy. This way the quality of reporting could be significantly improved, providing the best possible evidence for health care providers, clinicians and laboratory professionals; to the best for the patient care.



### 13. Illustrative Examples

To illustrate these, for our first example we shall use data from a study of diabetic eye tests (Harding *et al.*, 1995). This was a cross-sectional study in which diabetic patients being screening for eye problems were examined using direct ophthalmoscopy (the test) and slit lamp stereoscopic biomicroscopy (the reference standard). A single sample of subjects all received both the diagnostic test and the reference standard test. The following table shows the results for all eye problems combined:

**Table 2. Reference standard**

	+Ve	-Ve	Total
+Ve	40	38	78
-Ve	5	237	242
Total	42	275	320

From this table we can calculate all diagnostic test statistics other than a ROC curve: sensitivity =  $40/45 = 0.89 = 89\%$ , specificity =  $237/275 = 0.86 = 86\%$ , LR (+ve test) =  $0.89/(1 - 0.86) = 6.4$ , LR (-ve test) =  $0.86/(1 - 0.89) = 7.8$ , OR =  $40 \times 237 / (38 \times 5) = 49.9$ , PPV =  $40/78 = 51\%$ , NPV =  $237/242 = 98\%$ . We shall now look at what these mean and how they were calculated. Sensitivity = the proportion of reference positive cases who are positive on the test = proportion of true cases that the test correctly identifies. Specificity = the proportion of reference negative cases who are negative on the test = proportion of true non-cases that the test correctly identifies. For eye disease in diabetics, there were 45 reference standard positive cases of whom 40 were positive on the test, 275 reference standard negative non-cases of whom 237 were negative on the test. Sensitivity =  $40/45 = 0.89 = 89\%$ , Specificity =  $237/275 = 0.86 = 86\%$ . A good test will have high sensitivity and high specificity. We are looking for values exceeding 80%, preferably 90% or 95%. Odds = number of positives divided by number of negatives. Odds ratio (OR) = odds in one group divided by odds in another. For eye disease in diabetics: Odds test +ve for those reference +ve =  $40/5 = 8.0$ , OR =  $(40/5)/(38/237) = 40 \times 237 / (38 \times 5) = 49.9$ . As the test and the reference standard should have a strong positive relationship, we expect the odds ratio to be much greater than 1.0. The likelihood ratio (LR) for a positive test = sensitivity/(1 - specificity). We use this as follows. If we start with the probability that a subject has the disease, which is the prevalence of the disease, we can convert this to odds: odds = prevalence/(1 - prevalence). Then if we test a subject from a population with this prevalence, we can estimate the odds of having the disease if the test is positive: odds of disease if test positive = odds of disease  $\times$  likelihood ratio. For eye disease in diabetics:

Likelihood ratio for a positive test =  $0.89/(1 - 0.86) = 6.4$ . Suppose the prevalence of eye problem in the local diabetic population is  $10\% = 0.10$ . The odds of eye problems is  $0.10/0.90 = 0.11$ . If a subject has a positive test, the odds of eye disease will be increased: odds of disease if test

positive =  $0.11 \times 6.4 = 0.70$ . This corresponds to a probability of eye disease = 0.41. (Probability = odds/(1 + odds)). Similarly, the likelihood ratio for a negative test = specificity/(1 - sensitivity). As before, if we start with the probability that the subject does not have the disease = 1 - prevalence of disease and convert to odds =  $(1 - prevalence)/prevalence$ , we can look at the effect on the odds of not having the disease if the test is negative: odds of not disease if test negative = odds of not disease  $\times$  likelihood ratio Likelihood ratio for a negative test =  $0.86/(1 - 0.89) = 7.8$ . Suppose the prevalence of eye problem in the local diabetic population is  $10\% = 0.10$ . The odds of no eye problems is  $0.90/0.10 = 9.0$ . If a subject has a negative test, the odds of no eye disease will be increased: odds of disease if test negative =  $9.0 \times 7.8 = 70.2$ . This corresponds to a probability of no eye disease = 0.986. The positive predictive value (PPV) is the proportion of test positives who are reference positive. The negative predictive value (NPV) is the proportion of test negatives who are reference negative. For eye disease in diabetics, there were 78 test positives of whom 40 were positive on the reference standard, 242 test negatives of whom 237 were negative on the reference standard. PPV =  $40/78 = 51\%$ , NPV =  $237/242 = 98\%$ .

Hence if a subject is positive on the test, the probability that eye disease will be found using the reference standard is 51%. If a subject negative on the test, the probability that no eye disease will be found using the reference standard is 98%. For a receiver operating characteristic (ROC) curve, we need a different example. Sanchini *et al.* (2005) looked at the early detection of bladder cancer using a test of elevated urine telomerase, an enzyme involved in cell proliferation. The reference standard was histologically confirmed bladder cancer. This was a case-control study conducted in 218 men: 84 healthy individuals and 134 patients at first diagnosis of histologically confirmed bladder cancer. Urine telomerase is a measurement taking a range of possible values rather the presence or absence of a sign. If we change the value of telomerase which we classify as elevated, this will change the sensitivity and specificity. We can do this and plot the sensitivity against the specificity to see how they vary together. For obscure historical reasons, it is usual to plot sensitivity against one minus specificity, also called the false positive rate. This is the ROC curve, a plot of sensitivity against 1 - specificity. (The name comes from telecommunications. As far as we are concerned, it is just a name.) This is the ROC curve of Sanchini *et al.* (2005): They have drawn two separate ROC curves, one for their whole sample and the other for men aged 75 years or older. Sensitivity increases as one minus specificity increase, i.e. as specificity decreases. We make our test more sensitive at the expense of making it less specific. We are looking for a compromise cut-off which will give both high sensitivity and high specificity. Sanchini *et al.* (2005) chose 50 as being a reasonable compromise between a test which is sensitive, so finding

most cases with the disease, and specific, so does not pick up a lot of people who do not have the disease. The diagnostic tests on a ROC curve do not have to be determined by a continuous measurement, though they often are. All we need to plot the curve is more than one test. Sanchini *et al.* (2005) also show a different, non-numerical test: urine cytology, not sensitive but fairly specific. For the detection of bladder cancer using as a test that urine telomerase > 50 against a reference standard of histologically confirmed bladder cancer, the 2 by 2 table is:

**Table 3. Reference standard**

	+Ve	-Ve	Total
+Ve	120	10	130
-Ve	14	74	88
Total	134	84	218

We can calculate most of the statistics as before: sensitivity =  $120/134 = 0.90 = 90\%$ , specificity =  $74/84 = 0.88 = 88\%$ . LR (+ve test) =  $0.90/(1-0.88) = 7.5$ . LR (-ve test) =  $0.88/(1-0.90) = 8.8$ . OR =  $120 \times 74 / (10 \times 14) = 63.4$

However, the row totals would be meaningless and they are not shown in the table. This is because we took two separate groups of subjects. The row totals will depend on what ratio of cases to controls we used. They do not tell us anything about how many people would be test positive or test negative. As a result, PPV and NPV cannot be found in this study. We cannot estimate PPV and NPV in a case-control study. Their values depend on the prevalence of the disease in the population being tested. See Bland (2004) for more information.

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